

# Sparse Coding Minimizing $\ell_0$ : Matching Pursuit

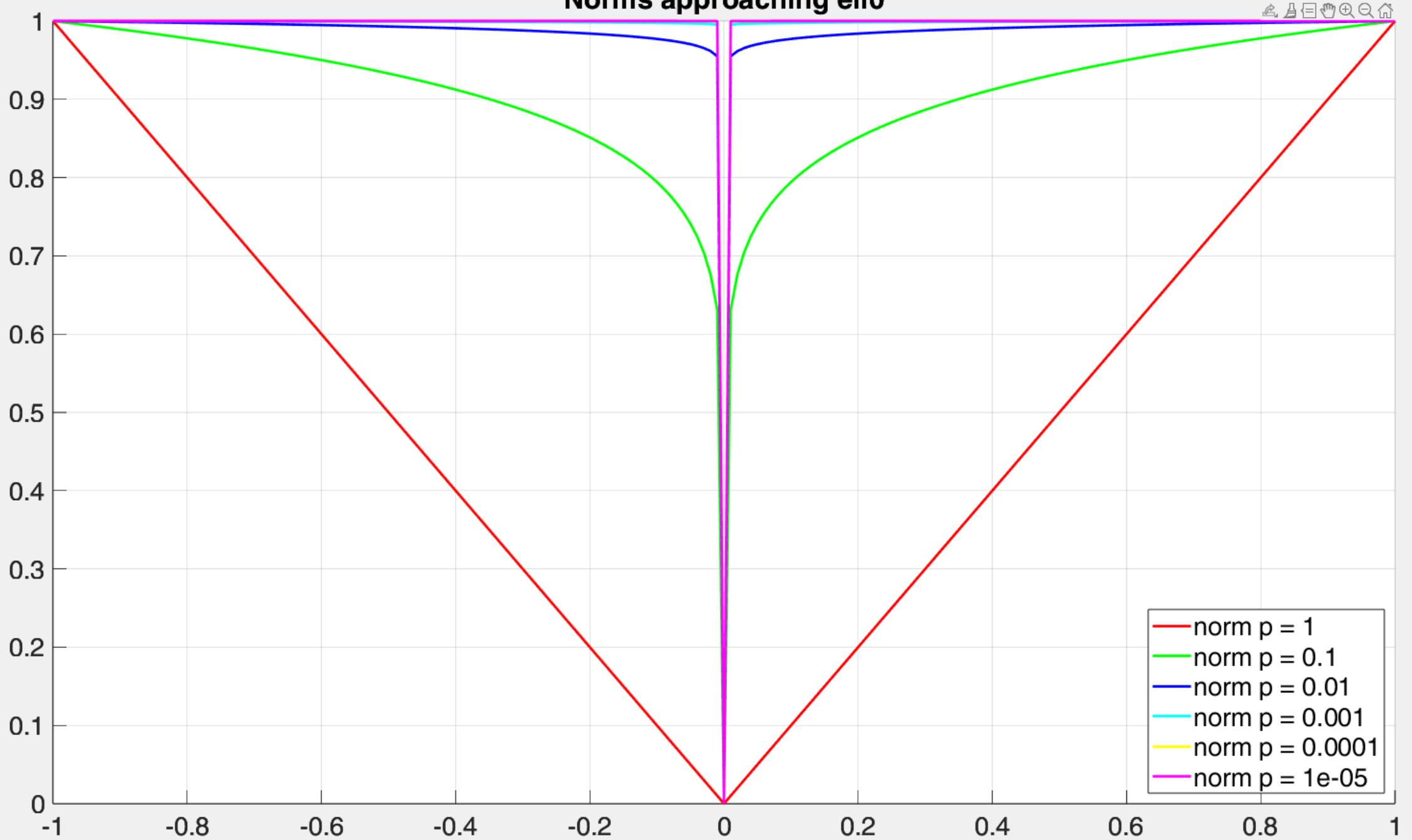
Mathematical Models and Methods for Image Processing

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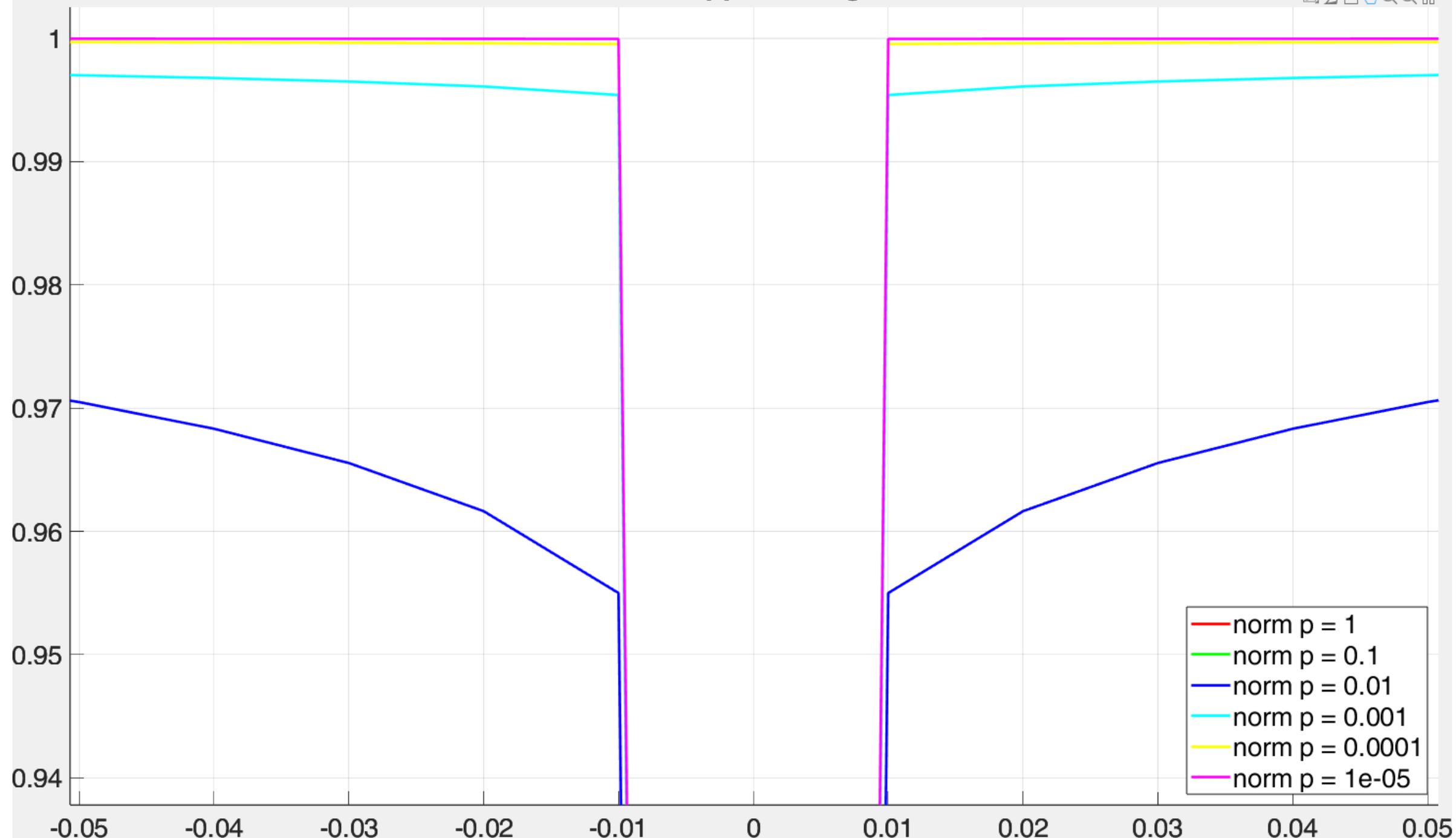
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# Norms approaching ell0



- norm  $p = 1$
- norm  $p = 0.1$
- norm  $p = 0.01$
- norm  $p = 0.001$
- norm  $p = 0.0001$
- norm  $p = 1e-05$

# Norms approaching ell0



# Assignment

Matching Pursuit

# Implement the Matching Pursuit

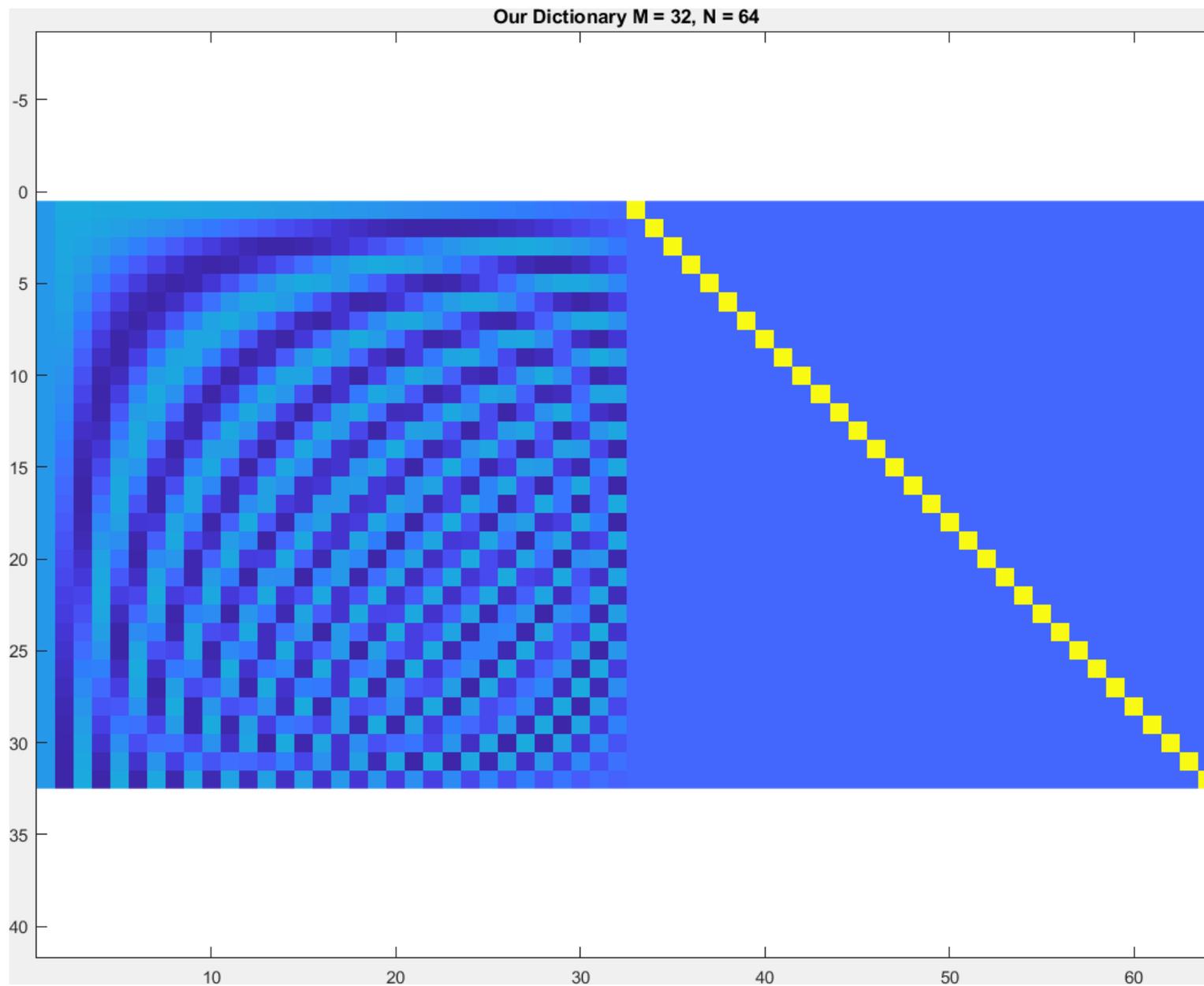
Take the setup of Assignment 5 and:

- Implement matching pursuit to solve

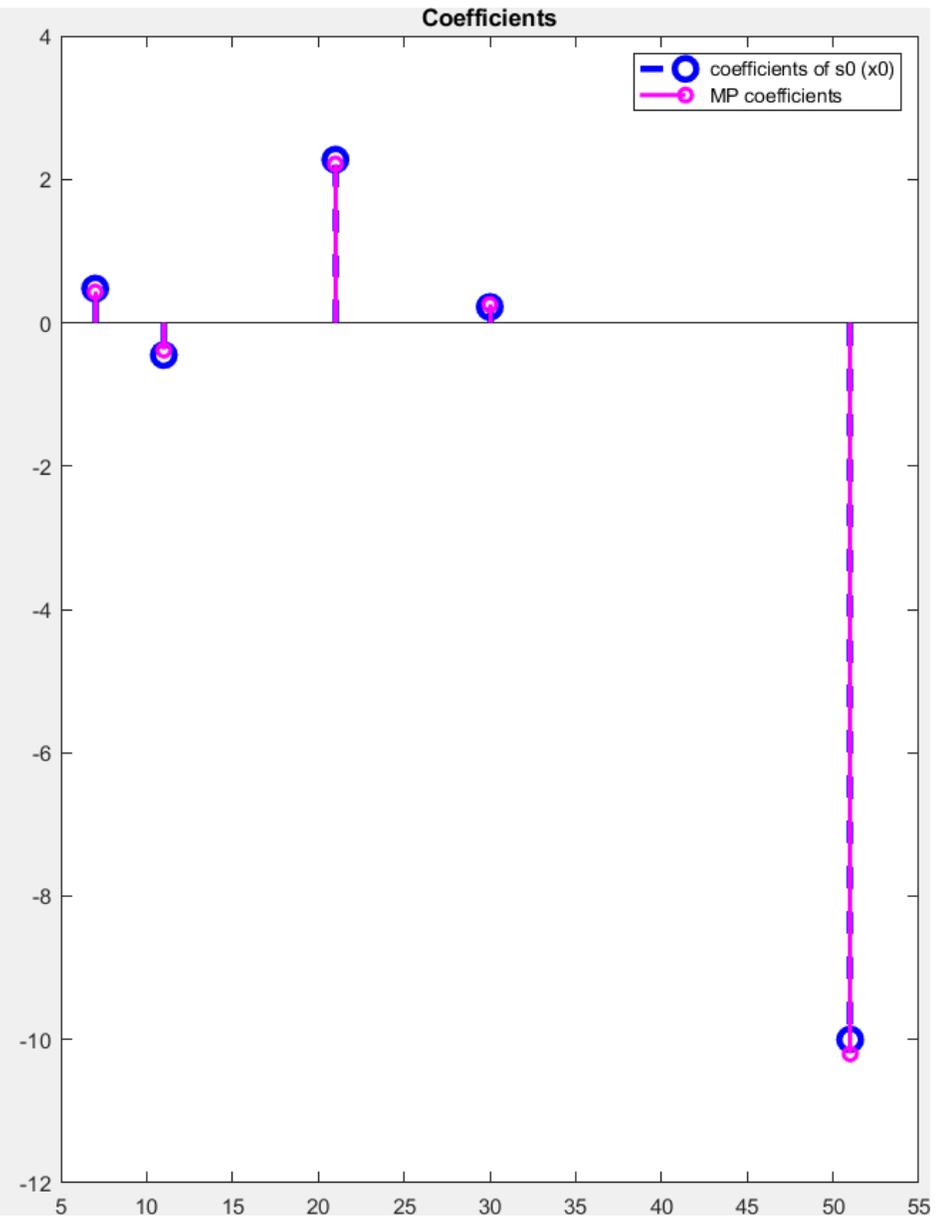
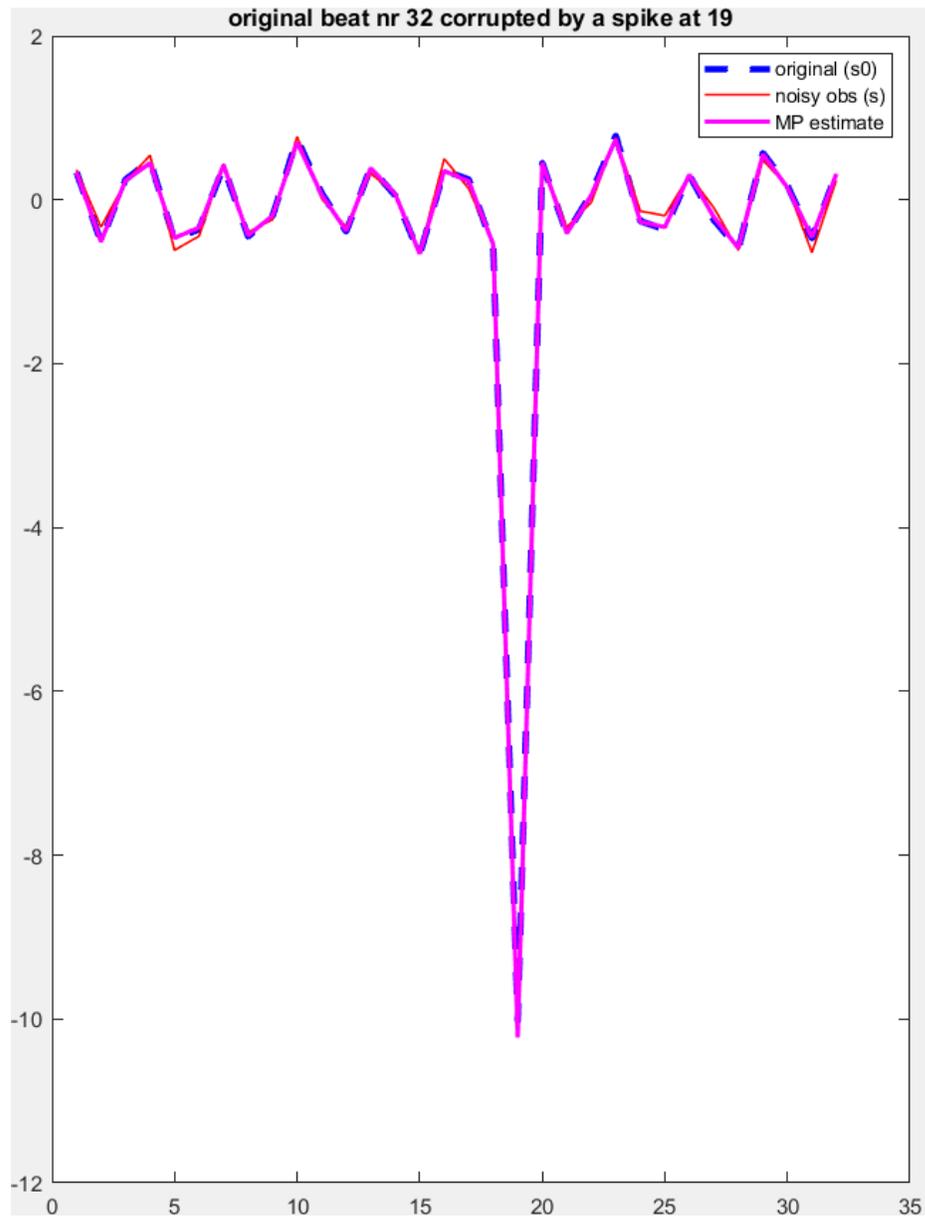
$$\hat{\mathbf{x}} = \underset{\mathbf{x} \in \mathbb{R}^M}{\operatorname{argmin}} \|\mathbf{x}\|_0 \quad \text{s.t.} \quad D\mathbf{x} = \mathbf{s}$$

- Where  $D = [DCT, C]$  and  $\mathbf{s}$  is an  $L$  –sparse signal w.r.t  $DCT$  and 1 –sparse signal w.r.t. the canonical basis  $C$
- Implement the Matching Pursuit algorithm and check the received support

# The Dictionary



# Results of Sparse Coding w.r.t. $D = [DCT, C]$



# Results of Orthogonal Projection over $DCT$

