# Wiener Filter

#### Mathematical Models and Methods for Image Processing

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#### **Empirical Wiener Filter**

Let  $\hat{y}^{HT}$  be the hard threshold estimate, with DCT coefficients:  $\hat{x}^{HT} = D^T \hat{y}^{HT}$ 

The empirical Wiener filter attenuates the DCT coefficients as:

$$\hat{x}_{i}^{Wie} = \frac{\left(\hat{x}_{i}^{HT}\right)^{2}}{\left(\hat{x}_{i}^{HT}\right)^{2} + \sigma^{2}} x_{i}$$

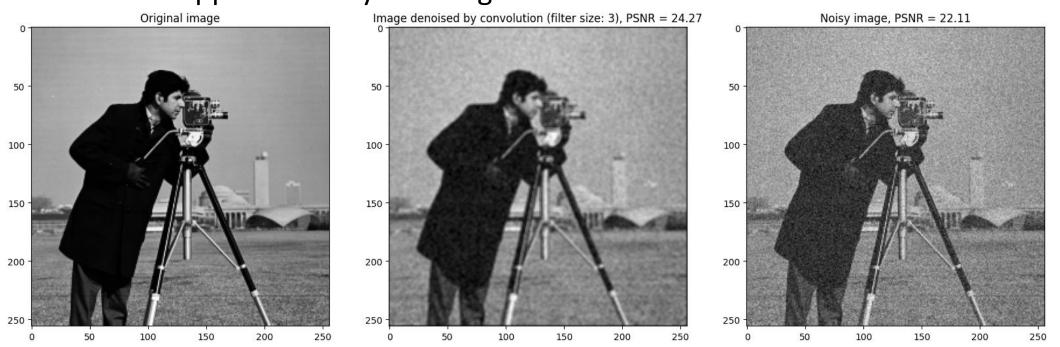
The empirical Wiener estimate is thus:

$$\widehat{y}^{Wie} = D \ \widehat{x}^{Wie}$$

## Assignments

### **Assignment 1– Baseline denoising**

- 1. Synthetically generate a noisy image (AWGN model)
- 2. Implement the noise level estimation method
  - 1. compare the robust vs non-robust standard deviation estimator
- 3. Perform denoising by convolution
  - 1. what happens when you change the kernel size?



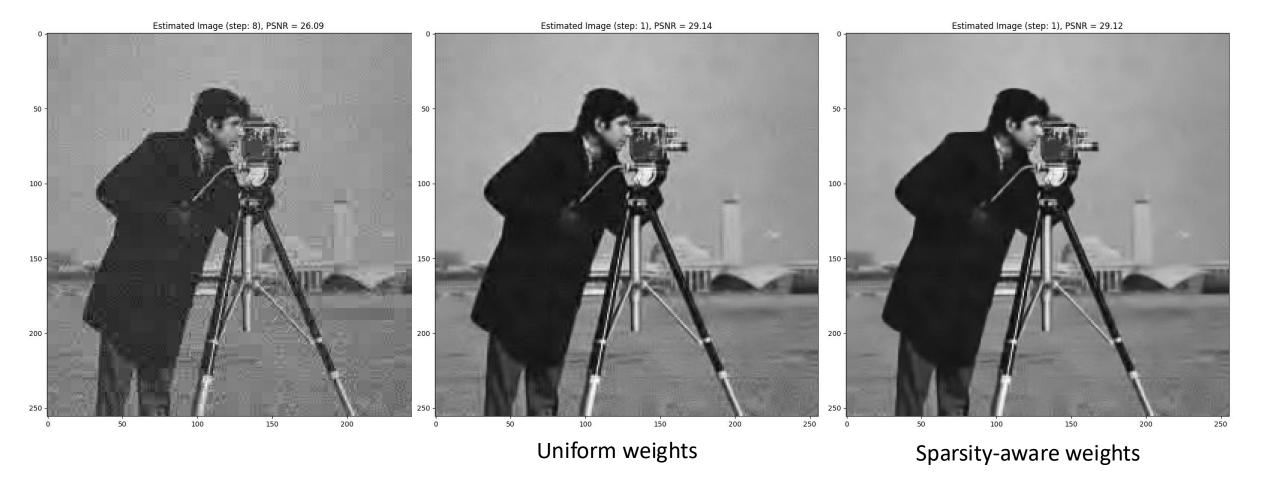
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## **Assignment 2 – Sliding DCT denoising**

- 1. Implement the sliding-DCT denoising using
  - no aggregation (operate on non-overlapping tiles)
  - aggregation using uniform weights
  - aggregation using weights inversely proportional to patch sparsity in DCT domain.
- 2. Test the three algorithms on both checkerboard and cameraman image
- 3. Test how much the choice of the threshold  $\tau$  influences the denoising performance. Observe the resulting image when:
  - $\tau \ll 3\sigma$
  - $\tau \gg 3\sigma$

This is very important to understand how important is the choice of the threshold

#### **DCT Denoising – Expected results**



#### **Assignment 3 – Wiener filter**

- 1. Compute a first estimate using DCT denoising with Hard Thresholding
- 2. Use this estimate to perform denoising via Wiener Filtering
  - Start with  $STEP = \sqrt{M}$  (non overlapping patches, as in JPEG)
  - Decrease the STEP and perform aggregation



