

# Local Polynomial Approximation

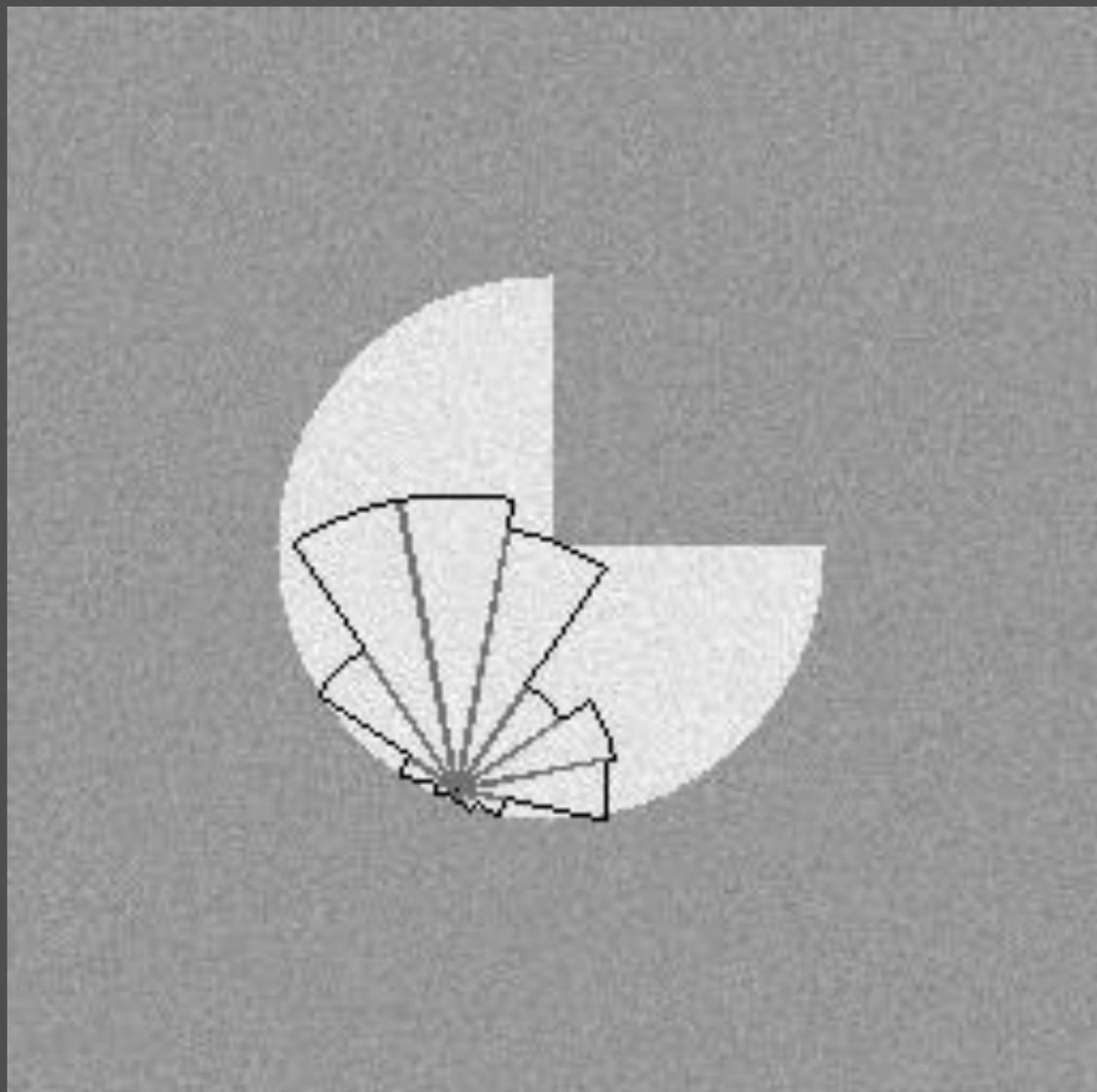
Mathematical Models and Methods for Image Processing

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[https://webpages.tuni.fi/foi/Present/Anis\\_Web.html](https://webpages.tuni.fi/foi/Present/Anis_Web.html)



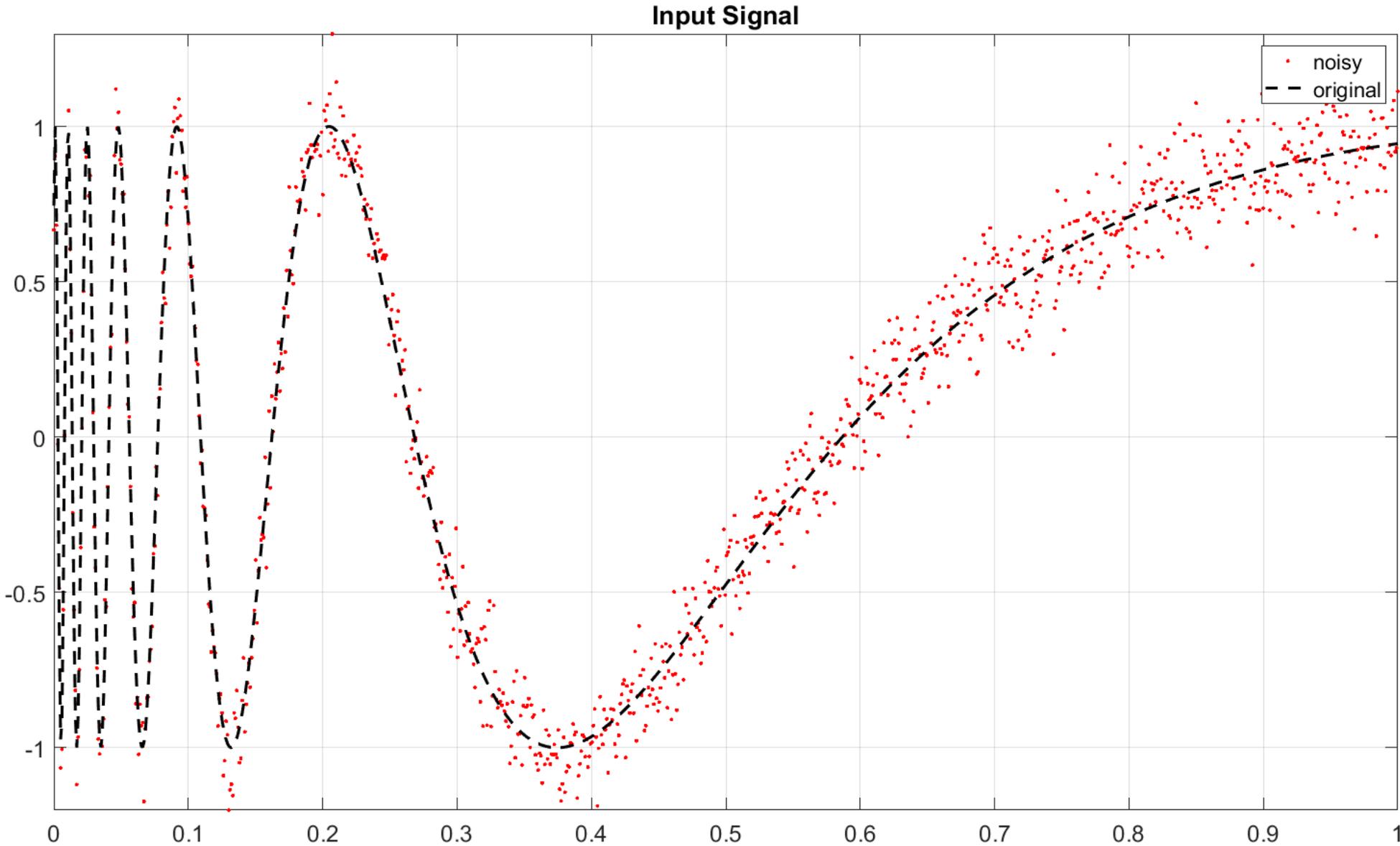
# **Assignment 1: LPA Kernels**

A. Foi, *Anisotropic nonparametric image processing: theory, algorithms and applications*, Ph.D. Thesis, Dip. di Matematica, Politecnico di Milano, April 2005.

# Lez21\_A\_LPA

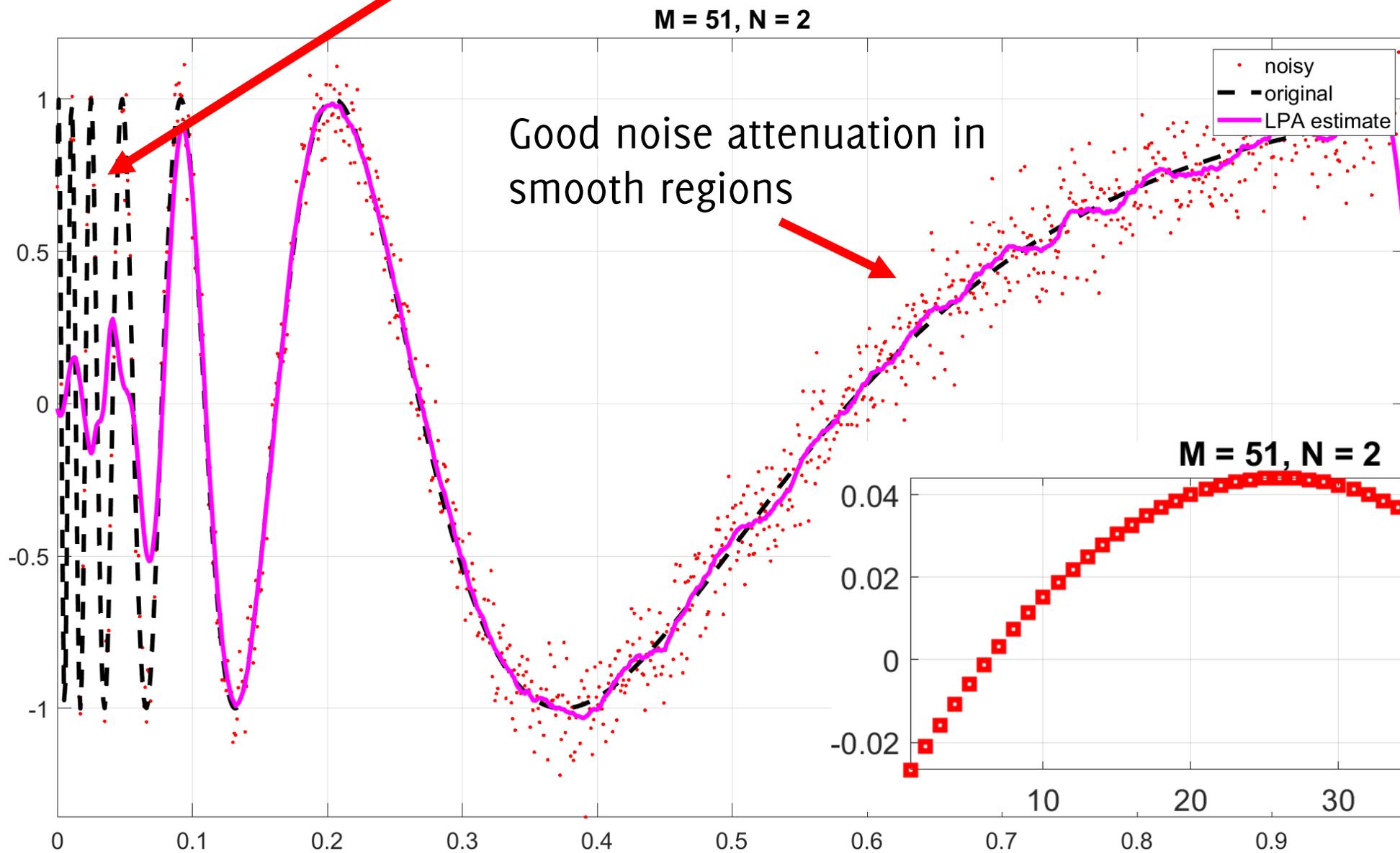
Define the LPA filters for a given polynomial order  $N$  and over a fixed support  $M$  to perform regression over noisy signals

# Noisy Signal



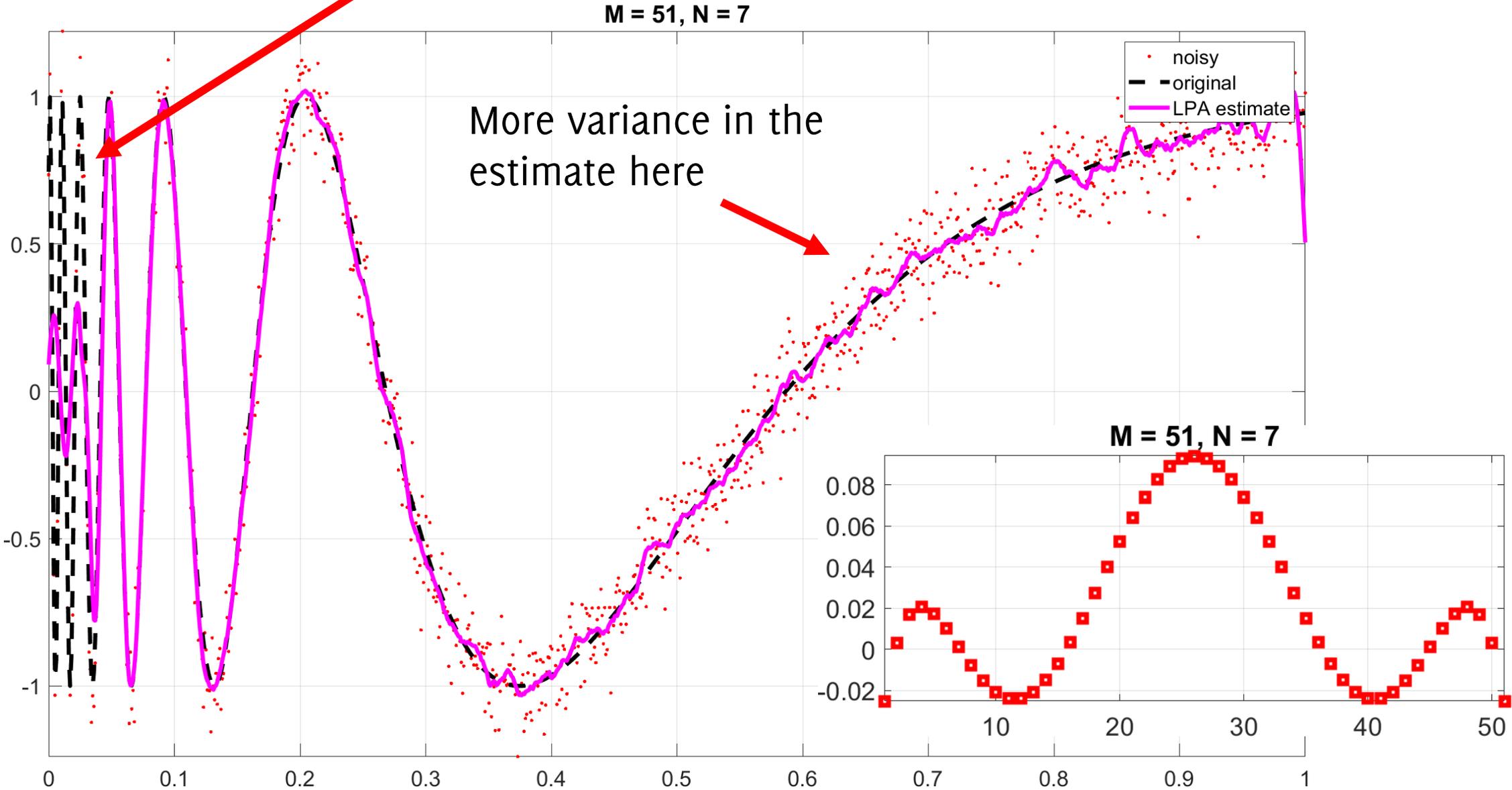
# Large $M$ , small $N$

Biased estimate when the signal frequency is high



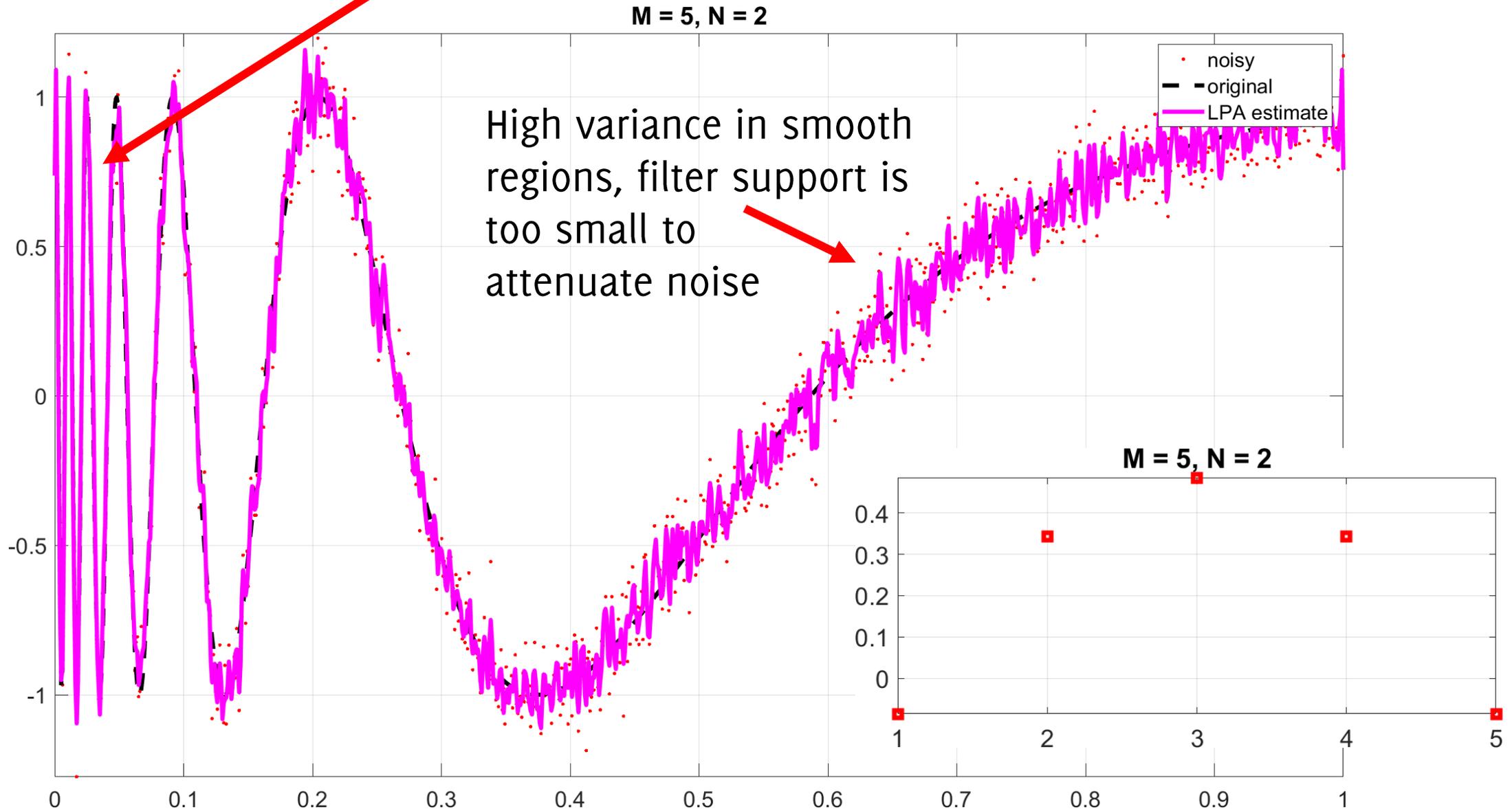
# Large $M$ , large $N$

Lower bias than before when the signal frequency is high



# small $M$ , small $N$

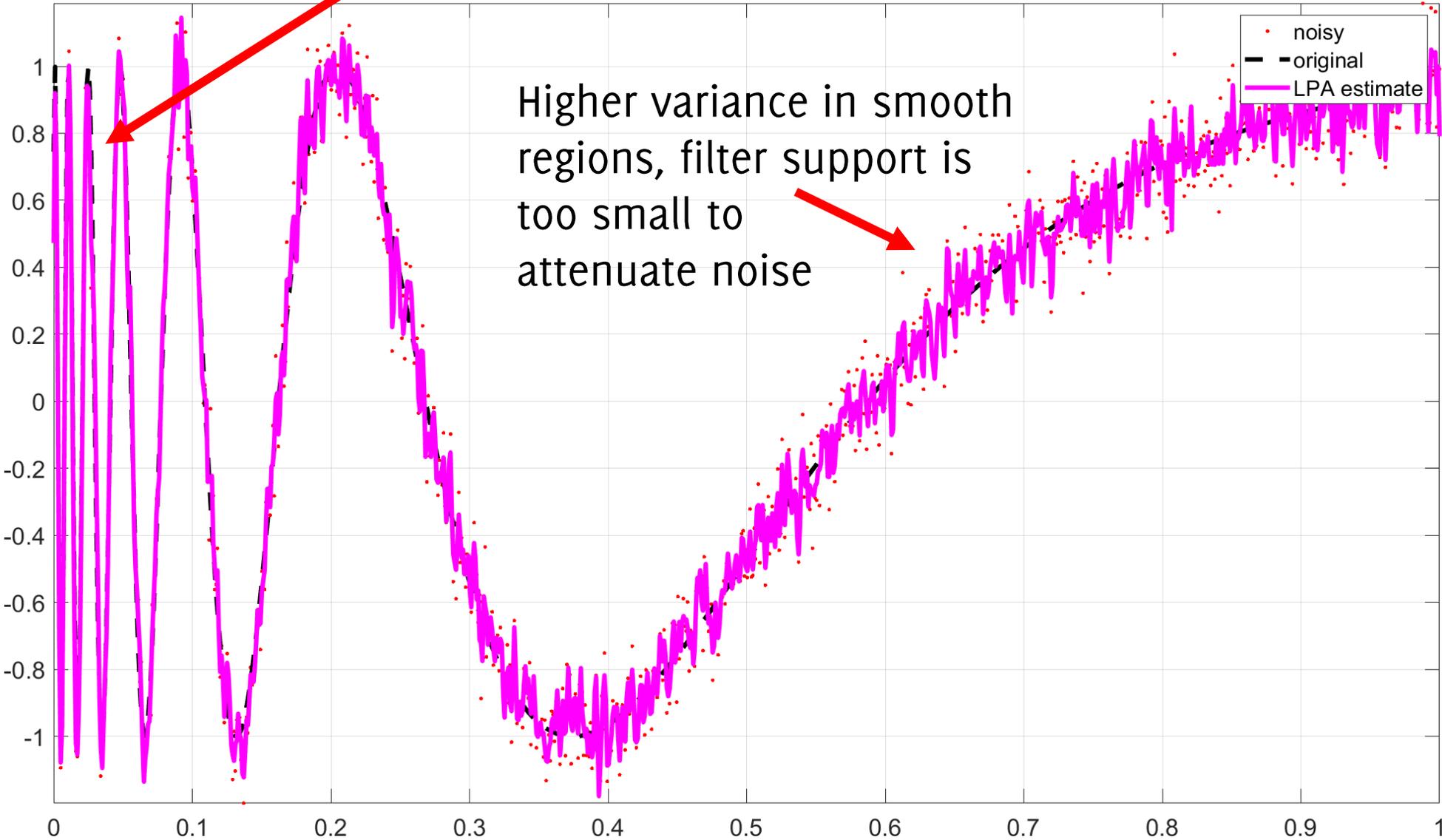
Lower bias than before when the signal frequency is high



# small $M$ , comparable $N$

Lower bias than before when the signal frequency is high

$M = 7, N = 5$



Higher variance in smooth regions, filter support is too small to attenuate noise

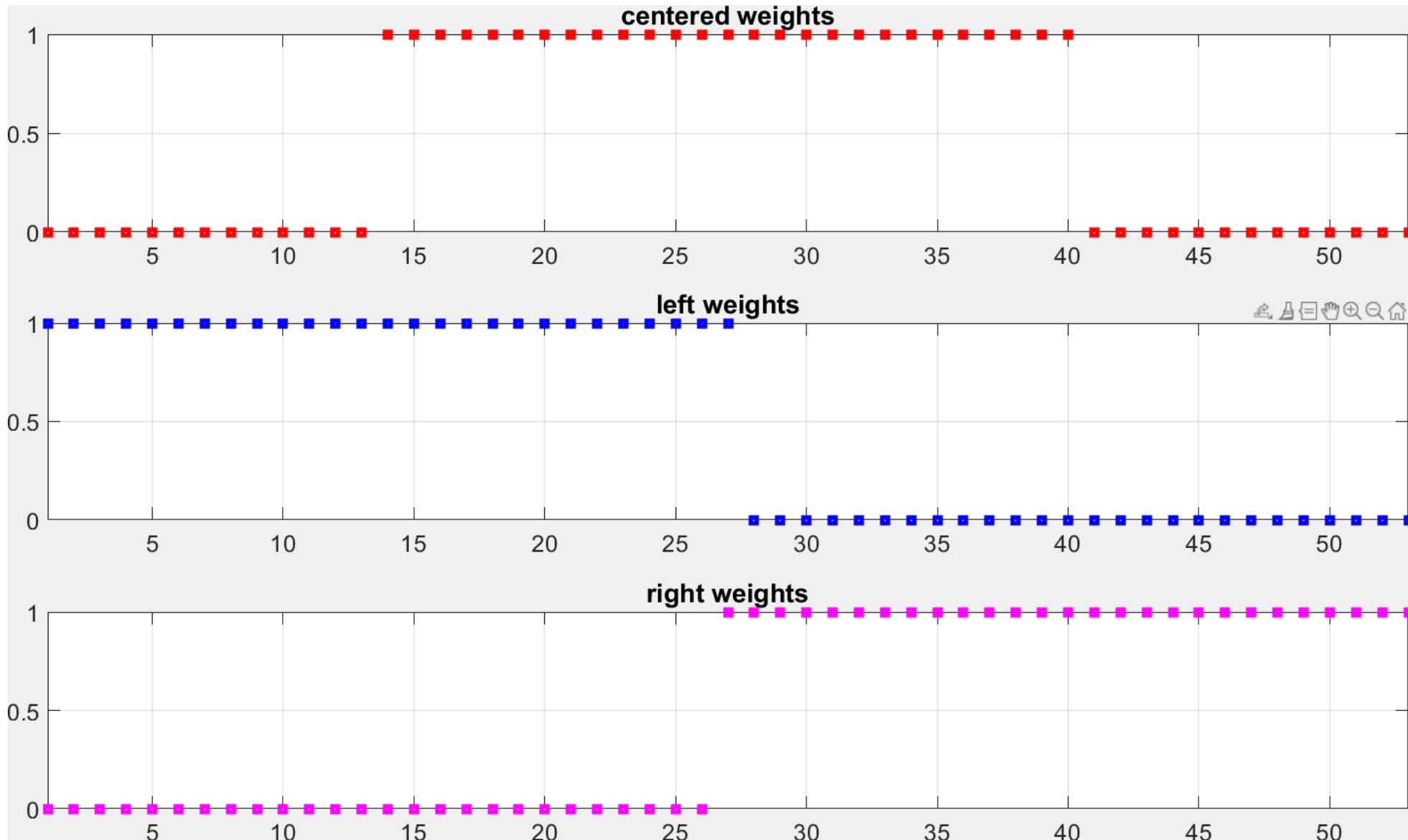
# **Assignment 2: Weighted LPA Kernels**

# Lez21\_B\_weighted\_LPA

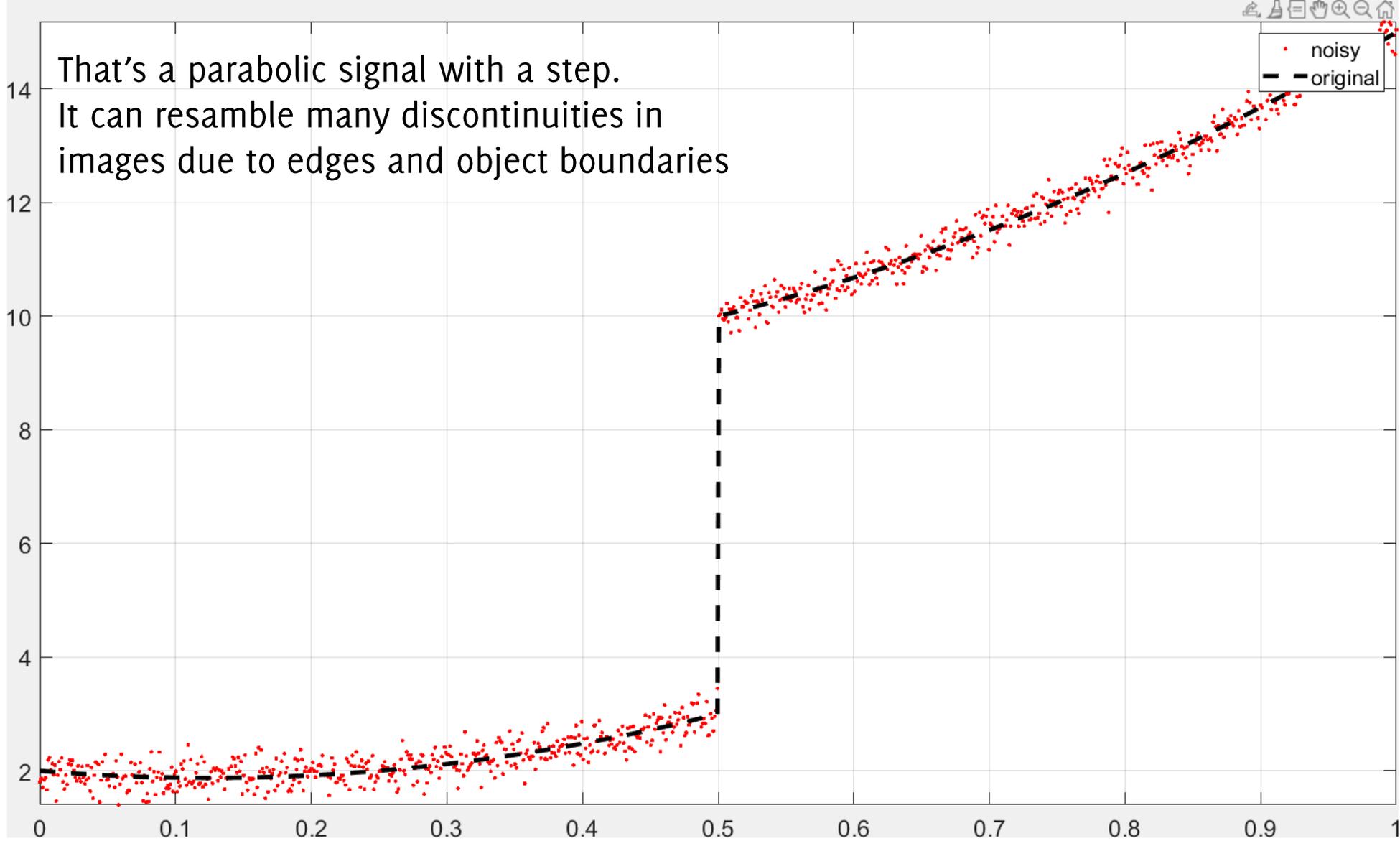
Define the **weighted LPA** filters for a given polynomial order  $N$  and over a fixed support  $M$  to perform regression over noisy signals

Use binary weights to compute centered, left and right estimates. See how these behave w.r.t. signal discontinuities

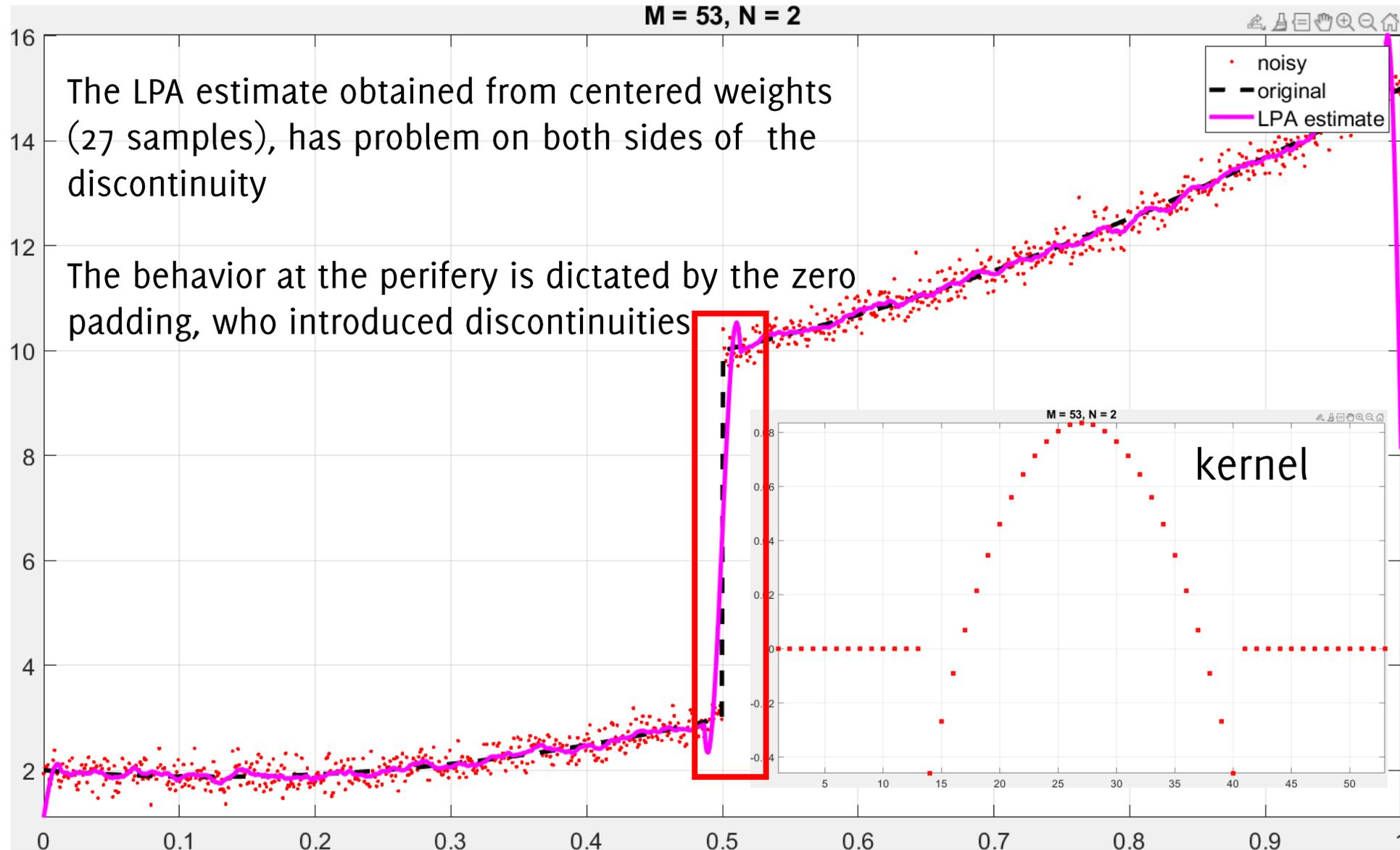
# Example of binary weights to use



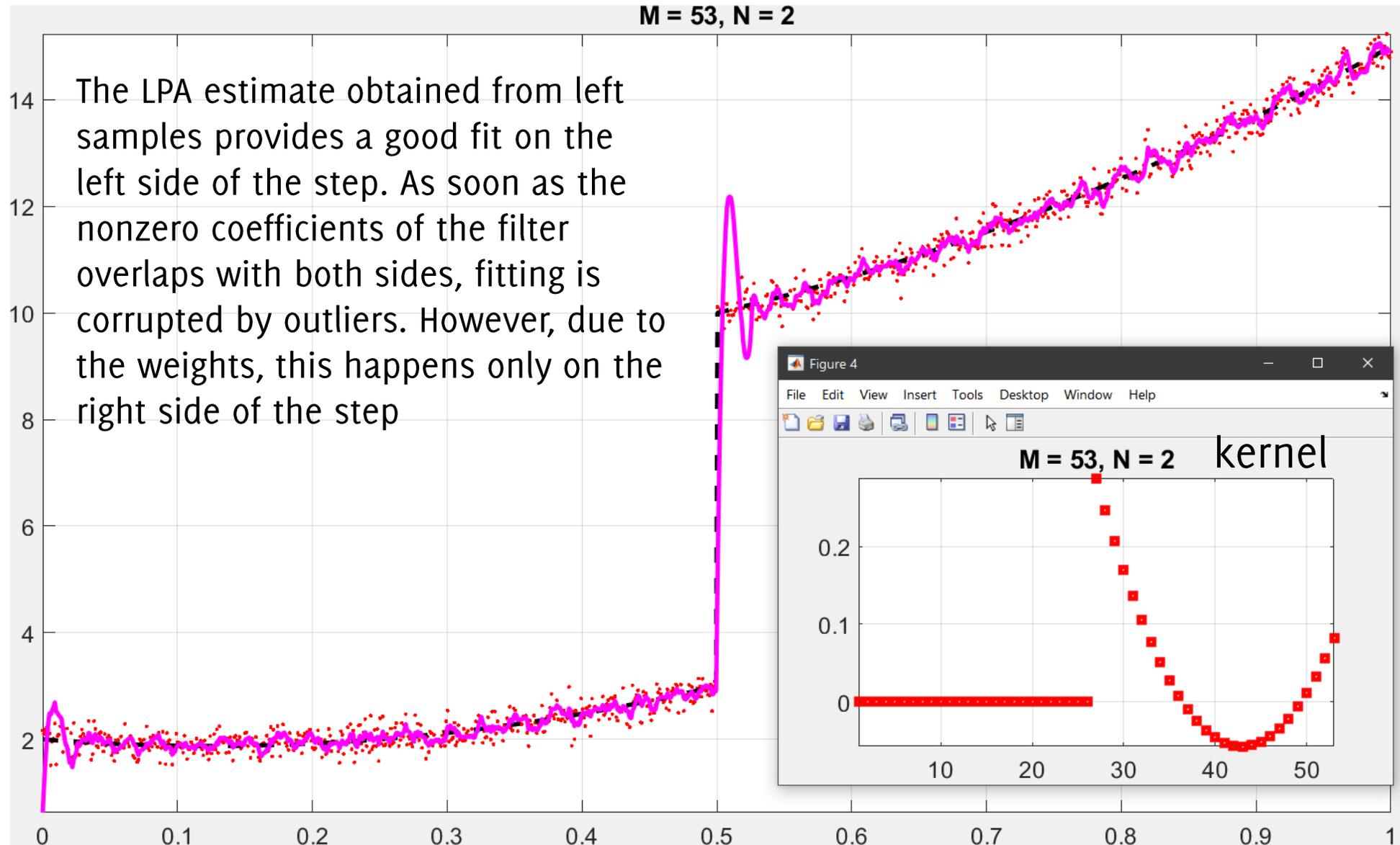
# Handling Discontinuities



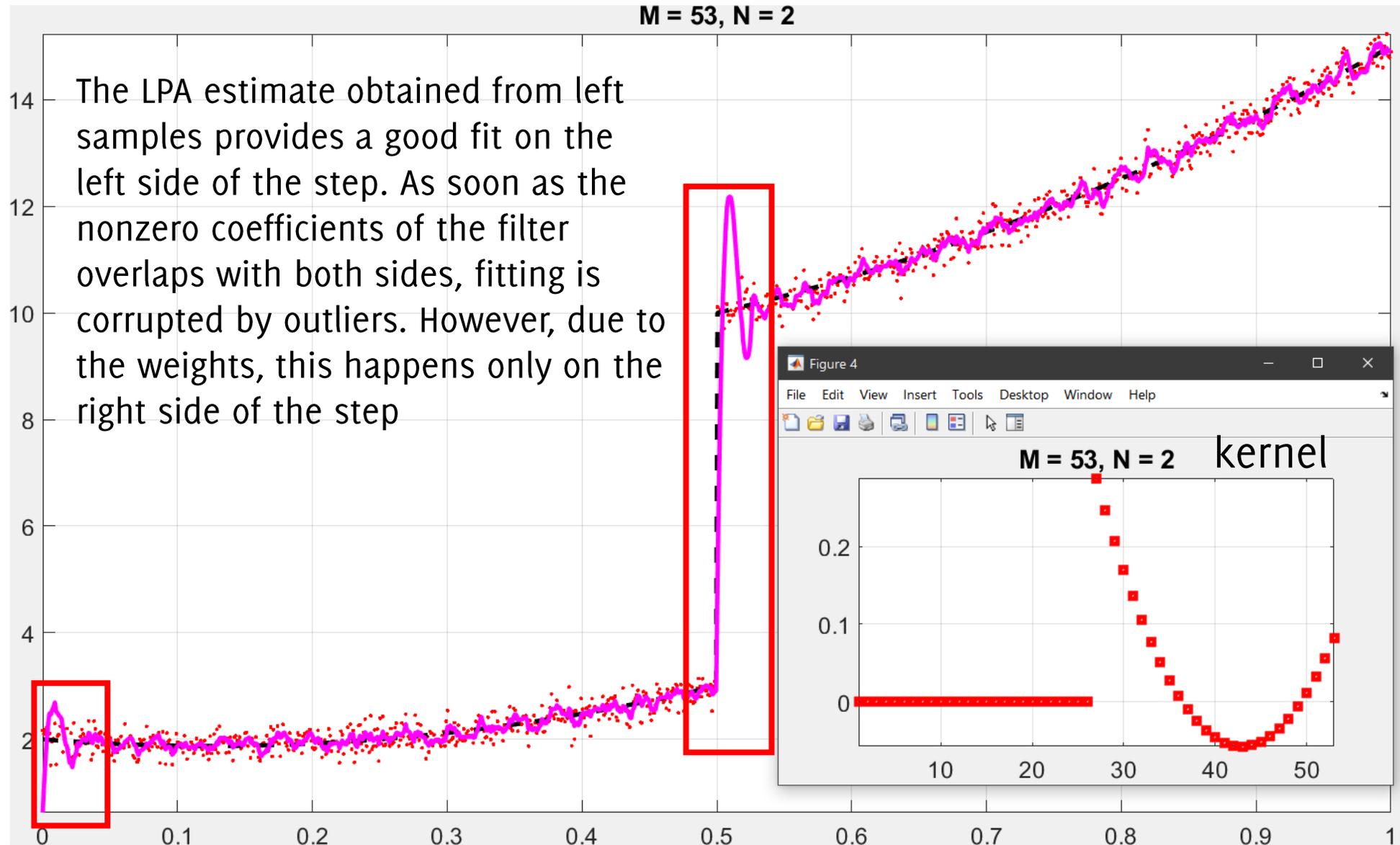
# Handling Discontinuities: «centered weights»



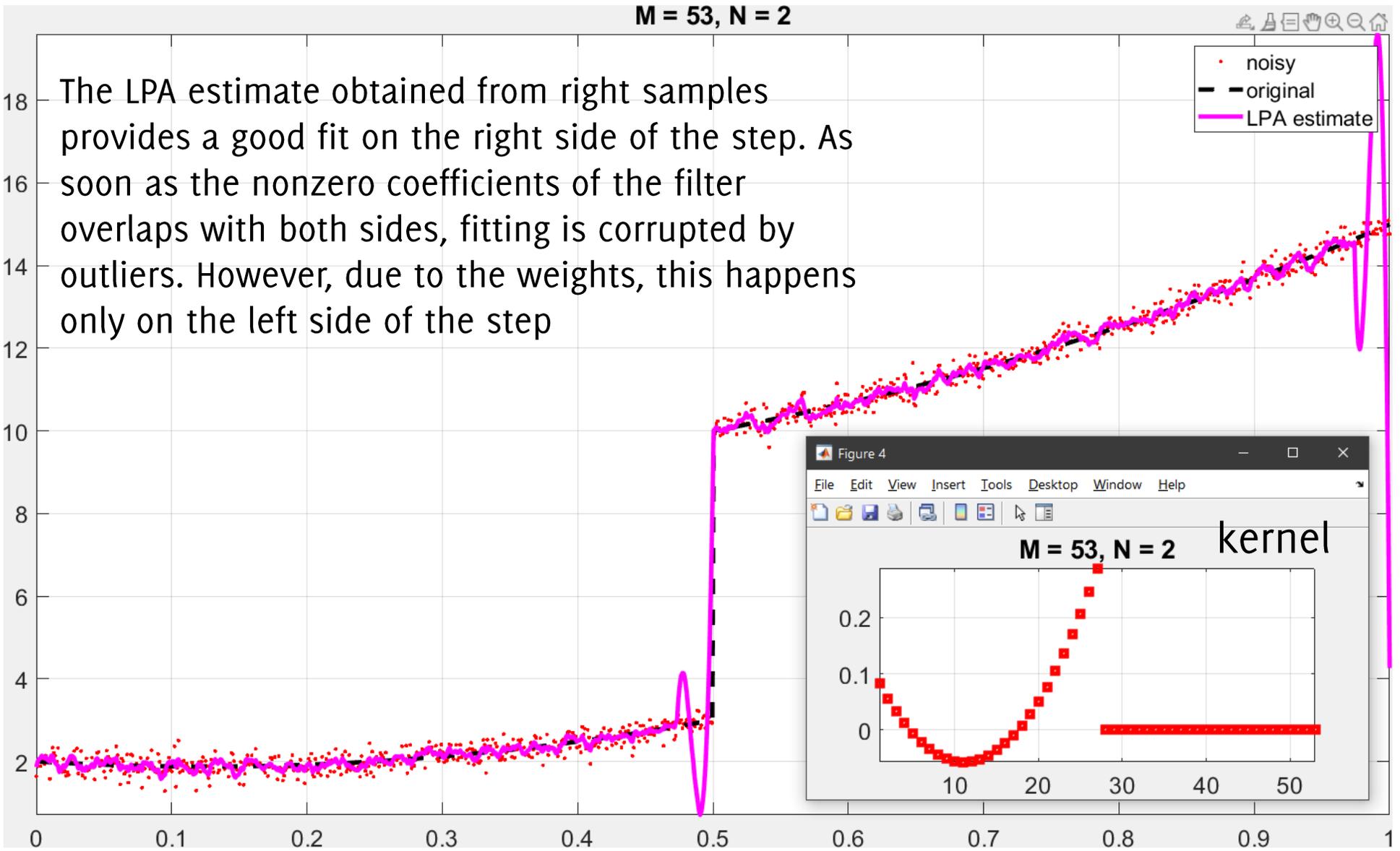
# Handling Discontinuities: «left weights»



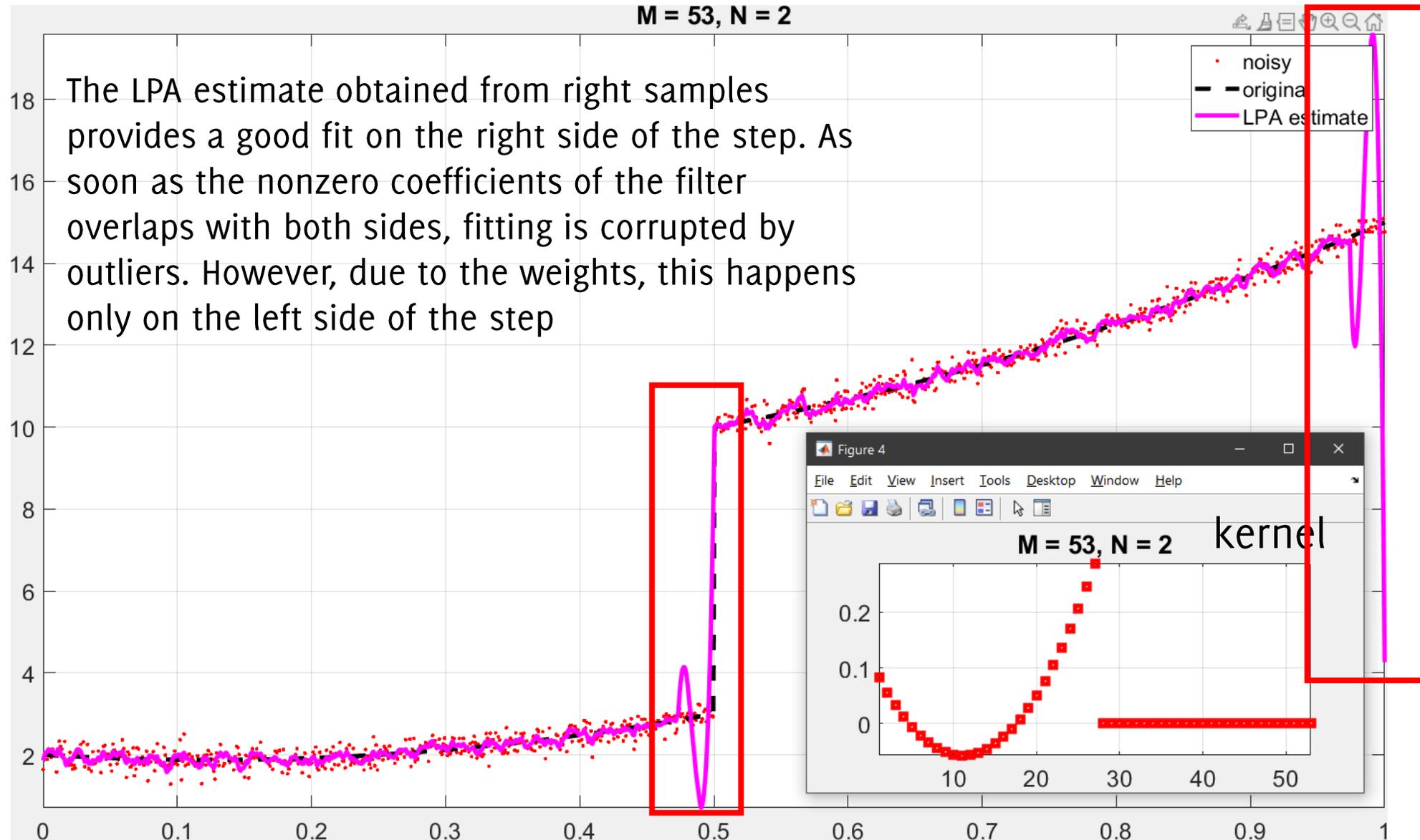
# Handling Discontinuities: «left weights»



# Handling Discontinuities: «right weights»



# Handling Discontinuities: «right weights»



# Handling Discontinuities: «right weights»

