

# Advanced Deep Learning Models and Methods for Spatial Data

Giacomo Boracchi, Luca Magri, Simone Melzi, Matteo Matteucci

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# **Depth estimation**

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## **Credits & acknowledgments**

Some of the material presented in these slides is based on

<u>Matteo Poggi</u>'s tutorial: Learning and understanding single image depth estimation in the wild, CVPR 2020 which is an excellent resource for approaching the problem of depth estimation.

The introductory material is inspired by <u>Justin Johnson</u>: *Deep learning for computer vision* (lecture 17)

Monodepth and material on self-supervision is based on the oral presentation done by <u>Clément Godard</u> at CVPR 2017.

Some slides are "stolen" from the AN2DL course of Prof. <u>Giacomo Boracchi</u>, who is kindly acknowledged here for his suggestions and support. Typically, the images are taken from the papers cited at the bottom of each slide.

The codes accompanying this lecture were provided by <u>Andrea Porfiri dal Cin</u>, whom I thank for his help.

Errors are my own! You are encouraged to report any of them to luca.magri@polimi.it

## **Motivations**

Navigation & mapping



Robot grasping



Augmented reality



#### Applications

- Robotics
- Autonomous Driving Assistive System
- Medical applications

## **Perceiving depth**

#### Active technologies

- Structured Light
- Time of Flight (TOF)
- Laser Image Detection Ranging (LiDAR)
- ✓ very accurate

#### LiDAR:

X Sparse measurementsX Expensive

Structured Light: X Can't work outdoor X Limited range

#### Passive technologies

- Binocular and multi-view stereo
- Structure from Motion

✓ cheap

Stereo: X Occlusions

SfM: X Moving objects

By estimating depth from a **single** image, we can bypass all these limitations!



# Depth estimation from a single image



## **Depth map**

Given a RGB image of size  $H \times W \times 3$ , we want to estimate

a **depth map**: an image of size  $H \times W$ that, for each pixel, gives the distance from the camera to the object in the world at that pixel.

#### **RGB image + Depth map = RGB-D image 2.5D**







far

close

# Depth from a single image is an ill posed problem

The capture of an image of a 3D scene is modelled as the **projection** of 3D points on a 2D image plane. All the points belonging to the optical ray projects on the same 3D points.

It is not possible to recover the depth of a point from a single image, as the **same image point** can be back-projected to **multiple plausible depths**.



# **Estimating depth form a single image is an ill posed problem!**



# Estimating depth form a single image is an ill posed problem!

#### Scale-depth ambiguity:

a small close object looks the same as a much larger one further away.

Absolute scale / depth is ambiguous from a single image





# Thank for your attention!

## ...but humans succeed estimating depth

however not all the 3D structures are equally likely! Humans are able to infer a (nearly) correct 3D structure and relative depth, using prior experience and visual cues such as:

- 1. Linear perspective
- 2. Relative size position
- 3. Texture gradient
- 4. Occlusions (the occluded object is far away)
- 5. Aerial perspective
- 6. Light and shadows
- 7. Blur/defocus



#### **Today menu**

 $\bigcirc$ 



#### Depth estimation from a **single image**

- Supervised methods
- Visual cues for single image depth estimation

#### Aims:



Get an intuition of the main approach for inferring 3D data from 2D images

Fill our box with the geometric tools necessary to depth estimation



#### Depth estimation from a **calibrated stereo pairs**

- Stereo self-supervision



• Mono-depth training & deep SfM



## **Supervised** approach



# **Supervised** approach









# From semantic segmentation to depths

A simple solution is to start with a Fully Convolutional Neural Networks as the one used for **semantic segmentation** 



# From semantic segmentation to depths

A simple solution is to start with a Fully Convolutional Neural Networks as the one used for **semantic segmentation** and **adapt** it to predict depth values instead of semantic labels.



- The **encoder** reduces the spatial extent of the image and produce deeper features that enode richer information
- The **decoder** upsamples the predictions to cover each pixel in the image at the original resolution



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- In semantic segmentation a soft-max to predict the proability of belonging to one of the L classes  $\Lambda =$  $\{l_1, ..., l_L\},\$
- To regress depth maps we have instead a linear layer.



- In semantic segmentation a soft-max to predict the proability of belonging to one of the L classes  $\Lambda = \{l_1, ..., l_L\}$ ,
- To regress depth maps we have instead a linear layer.

Linear activations



# **Other architectures**

Most of the architectures for supervised depth estimation from a single image are based on this encoder-decoder paradigm, keeping this in mind you should be able to navigate the literature...

#### *e.g.,* Adabins



Bhat, Shariq Farooq, Ibraheem Alhashim, and Peter Wonka. "Adabins: Depth estimation using adaptive bins." CVPR 2021.

#### A naïve loss

As a loss, we could minimize the  $\ell_2$  norm between the predicted and the regressed v







#### A naïve loss

Inr

As a loss, we could minimize the  $\ell_2$  norm between the predicted and the regressed v

But this v To predic



cause of the **depth-scale ambiguity**!

re must consider the **geometric nature** of the problem



#### A naïve loss

As a loss, we could minimize the  $\ell_2$  norm between the predicted and the regressed v



# Back to the roots: a CNN for single image depth estimation

[Eigen et al, NIPS 2014] is a milestone in single image depth estimation, being the first work leveraging a CNN to estimate the depth in a *supervised* way.

• While stereo methods rely on local disparity (see later), in single image depth estimation a **global view** is needed to relate all the available visual cues.

Two-branch architecture: global and fine scale

• One of the major ambiguity is the global scale of the scene (moderate variations in room furniture and size).



Scale invariant loss





Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

# **Model architecture**

Two branches estimate a coarse and a refined depth maps, the former used as to ease the prediction of the latter.



#### **Coarse-scale Network:**

Global understanding thanks to:

- Max pooling to combine information from different part of the image
- Fully connected layers to contain the entire image in their receptive field.
- Layers 1-5 pretrained on ImageNet



Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

# **Model architecture**

Two branches estimate a coarse and a refined depth maps, the former used as to ease the prediction of the latter.



#### **Fine-scale Network:**

Local refinement to align coarse prediction to local details such as object and walls.



Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

The scale invariant loss focus on the spatial relations within a scene rather than on



Scale invariant loss

tion from a Single Image using a Multi-Scale Deep Network, NIPS 2014





The scale invariant loss focus on the spatial relations within a scene rather than on a global scale:

$$D(y, y^*) = \frac{1}{n} \sum_{i=1}^n \left( \log y_i - \log y_i^* + \alpha(y, y^*) \right)^2$$

Mean squared error



Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

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Log space: reduces the impact of large depth values overpowering the smaller ones in error calculation.



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 Mean squared error

Log space: reduces the impact of large depth values overpowering the smaller ones in error calculation.

Scale invariant:  $\alpha(y, y^*) = \frac{1}{n} \sum_{i=1}^{n} (\log y_i - \log y_i^*)$  is the value that minimizes the error for a given pair  $(y, y^*)$ . For any prediction  $y, e^{\alpha}$  is the scalar that best align it to the groundtruth.

All scalar multiples of *y* have the same error, here the scale invariance.





Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

## Scale invariant

The scale invariant loss focus on the spatial relations within a scene rather than on a global scale:

$$D(y, y^*) = \frac{1}{n} \sum_{i=1}^{n} \left( \log y_i - \log y_i^* + \alpha(y, y^*) \right)^2$$
  
Mean squared error

The loss has other equivalent forms, i.e:

$$D(y, y^*) = \frac{1}{n^2} \sum_{i,j} \left( \left( \log y_i - \log y_j \right) - \left( \log y_i^* - \log y_j^* \right) \right)^2$$

to have low error, each pair of pixel in the prediction must differ in depth by an amount that is comparable to the ground truth. Setting  $d_i = \log y_i - \log y_j$ , we have

$$D(y, y^{*}) = \frac{1}{n} \sum_{i} d_{i}^{2} - \frac{1}{n} \left( \sum_{i} d_{i} \right)^{2}$$

Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

Luca Magri 2024

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# Scale invariant loss mean squared error in log space

The scale invariant loss focus on the spatial relations within a scene rather than on a global scale:

$$D(y, y^*) = \frac{1}{n} \sum_{i=1}^{n} \left( \log y_i - \log y_i^* + \alpha(y, y^*) \right)^2$$
Mean

Mean squared error

The loss has other equivalent forms, i.e:

$$D(y, y^*) = \frac{1}{n^2} \sum_{i,j} \left( \left( \log y_i - \log y_j \right) - \left( \log y_i^* - \log y_j^* \right) \right)^2$$

to have low error, each pair of pixel in the prediction must differ in depth by an amount that is comparable to the ground truth. Setting  $d_i = \log y_i - \log y_j$ , we have

$$D(y, y^*) = \frac{1}{n} \sum_{i} d_i^2 - \frac{\lambda}{n} \left( \sum_{i} d_i \right)^2$$

The loss used during training is a linear combination  $\lambda = 0.5$  of the mean square error and the invariant loss

Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

#### **Other losses**



J. Hu, et al. Revisiting single image depth estimation: Toward higher resolution maps with accurate object boundaries. In WACV, 2019.
#### Loss on gradients

Let  $\nabla_x d_i$  and  $\nabla_y d_i$  be the horizontal and vertical image gradients of the log difference  $d_i = \log y_i - \log y_i^*$ 

$$l_{\text{grad}} = \frac{1}{n} \sum \left[ (\nabla_x d_i)^2 + (\nabla_y d_i)^2 \right]$$

compares image gradients of the prediction with the ground truth.

This encourages predictions to have

- close values,
- but also similar local structure,

resulting in depthmaps that better follow depth gradients, with no degradation in measured l2 performance.



Eigen et al. Depth Map Prediction from a Single Image using a Multi-Scale Deep Network, NIPS 2014

#### Loss on normals

Depth can be seen as a surface z = z(x, y) defined on the image pixel gird (x, y)

The normal in (x, y) can be computed from the depth by taking the cross product between the tangent vectors to z(x, y).

(Viceversa, from normals it is possible to retrieve the depth by integration)

Let n and  $n^*$  be the estimated and the predicted normals

 $l_{norm} = \cos(n, n^*)$ 





Depth (lo<u>ss on depth and gradients</u>)



Eigen et al. Depth Ma Deep Network, NIPS 2



Depth







#### ormal and semantic labels

e image typically requires several images of the same scene acquired under ation conditions (this problem is known as **Photometric Stereo**).

Normals



#### The benefits of combining losses



Input photo

Output w/o  $\mathcal{L}_{\mathsf{grad}}$ 

Output w/  $\mathcal{L}_{grad}$ 



Zhengqi Li and Noah Snavely. "MegaDepth: Learning Single-View Depth Prediction from Internet Photos» CVPR18.

#### The benefits of combining losses



Input photo

Output w/o  $\mathcal{L}_{ord}$ 

Output w/  $\mathcal{L}_{ord}$ 



Zhengqi Li and Noah Snavely. "MegaDepth: Learning Single-View Depth Prediction from Internet Photos» CVPR18.

#### **Evaluation metrics**

• Accuracy scores: the percentage of pixels having a relative error  $\delta$  lower than a threshold  $\epsilon$  (typical values of  $\epsilon$  are 1,25, 1.25<sup>2</sup>, 1.25<sup>3</sup>)

$$\delta = \max\left(\frac{y}{y^*}, \frac{y^*}{y}\right) < \epsilon$$

• Absolute Relative error: to normalize per-pixel errors according to real depth, reducing the impact of large errors with the distance

$$\frac{1}{n}\sum |y_i - y_i^*| / y_i^*$$

• Squared Relative Error: to penalize larger depth errors (e.g. near discontinuities)

$$\frac{1}{n} \sum ||y_i - y_i^*||^2 / y_i^*$$

- Root Mean Squared Error:  $\sqrt{\frac{1}{n}\sum ||y_i y_i^*||^2}$
- Roor Mean Squared Logarithmic Error:  $\sqrt{\frac{1}{n}\sum ||\log y_i \log y_i^* * ||^2}$

#### **3D data for supervision**

A training set

 $TR = \{(I_i, , Y_i)\}$ 

of RGB-D image can be acquired using dedicated sensors.





## Why depth from a single image?

What is the advantage of having a deep network (4K€ for a GPU) that works on a single image rather than using a sensor that costs a few hundred €?

There are good reasons... would you rather have a Kinect or a small endoscopic probe in your belly?

We can rely on deep network when acquiring 3D data is not possible!





## The need of 3D data for supervision (and where to find them)

Deep learning method have recently driven significant progress in supervised depth estimation from a single image, but being entirely data driven, their potential grows with the amount of data using during training.

#### Popular datasets:

Dataset	Indoor	Outdoor	Dynamic	Video	Dense	Accuracy	Diversity	Annotation	Depth	# Images
DIML Indoor [31]	] 🗸			1	✓	Medium	Medium	RGB-D	Metric	220K
MegaDepth [11]		$\checkmark$	(✔)		(✔)	Medium	Medium	SfM	No scale	130K
ReDWeb [32]	$\checkmark$	$\checkmark$	$\checkmark$		$\checkmark$	Medium	High	Stereo	No scale & shift	3600
WSVD [33]	$\checkmark$	$\checkmark$	$\checkmark$	✓	$\checkmark$	Medium	High	Stereo	No scale & shift	1.5M
3D Movies	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	$\checkmark$	Medium	High	Stereo	No scale & shift	75K
DIW [34]	1	1	1			Low	High	User clicks	Ordinal pair	496K
ETH3D [35]	1	$\checkmark$			$\checkmark$	High	Low	Laser	Metric	454
Sintel [36]	1	$\checkmark$	$\checkmark$	1	$\checkmark$	High	Medium	Synthetic	(Metric)	1064
KITTI [28], [29]		$\checkmark$	(✔)	✓	(✔)	Medium	Low	Laser/Stereo	Metric	93K
NYUDv2 [30]	1		(✔)	✓	$\checkmark$	Medium	Low	RGB-D	Metric	407K
TUM-RGBD [37]	1		(✔)	$\checkmark$	$\checkmark$	Medium	Low	RGB-D	Metric	80K



Ranftl et al. Towards Robust Monocular Depth Estimation: Mixing Datasets for Zero-shot Cross-dataset Transfer. TPAMI 2020

#### NYU v2

Video sequences form a variety of indoor scenes acquired with a Microsoft Kinect to record both the RGB and Depth Map.

- 1449 densely labeled pairs of aligned RGB and depth images
- 464 new scenes taken from 3 cities
- 407,024 new unlabeled frames
- Each object is labeled with a class and an instance number (cup1, cup2, cup3, etc)

Dataset	Indoor	Outdoor	Dynamic	Video	Dense	Accuracy	Diversity	Annotation	Depth	# Images
DIML Indoor [31]	] 🗸			1	1	Medium	Medium	RGB-D	Metric	220K
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ReDWeb [32]	1	✓	✓		1	Medium	High	Stereo	No scale & shift	3600
WSVD [33]	1	✓	✓	1	1	Medium	High	Stereo	No scale & shift	1.5M
3D Movies	1	✓	$\checkmark$	1	✓	Medium	High	Stereo	No scale & shift	75K
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TUM-RGBD [37]	1		(✔)	1	1	Medium	Low	RGB-D	Metric	80K



https://cs.nyu.edu/~silberman/d atasets/nyu\_depth\_v2.html

#### **KITTI dataset**

A large collection of images acquired in driving environment.

3D point cloud acquired by a LiDAR registered with RGB.

A subset of 200 images (KITTI 2015 stereo training set) with accurate ground truth (moving object replaced with accurate cad model)



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https://www.cvlibs.net/data sets/kitti/

#### MegaDepth

A large scale dataset generated from Internet photo collections for a set of well-photographed landmarks.

The idea is to feed multiple images with overlapping viewpoint to **Structure from Motion** and **Multi-view Stereo** to automatically produce depth maps.

Multiple filtering steps are necessary.

3D data is only up to unknown scale factor, which could be problematic for applications requiring scaled values.

Dataset	Indoor	Outdoor	Dynamic	Video	Dense	Accuracy	Diversity	Annotation	Depth	# Images
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TUM-RGBD [37]	] 🗸		( <b>v</b> )	1	1	Medium	Low	RGB-D	Metric	80K



**Rialto Bridge**, Venice

Eiffel Tower, Paris









Parthenon, Athens

Florence Cathedral, Florence



https://www.cs.cornell.edu/pro jects/megadepth/

#### **Depth anything**



Figure 1. Our model exhibits impressive generalization ability across extensive unseen sce SA-1B [27] (a hold-out unseen set). **Right two:** photos captured by ourselves. Our model 3rd column), complex scenes (2nd and 5th column), foggy weather (5th column), and ult

#### Abstract

#### 1. Introduct

This work presents Depth Anything<sup>1</sup>, a highly practical solution for robust monocular depth estimation. Without pursuing novel technical modules, we aim to build a simple yet powerful foundation model dealing with any images under any circumstances. To this end, we scale up the dataset by designing a data engine to collect and automatically annotate large-scale unlabeled data ( $\sim$ 62M), which significantly enlarges the data coverage and thus is able to reduce the generalization error. We investigate two simple yet effective strategies that make data scaling-up promising. First, a more challenging optimization target is created by leveraging data augmentation tools. It compels the model to actively seek extra visual knowledge and acquire robust representations.

The field of cor is currently exp "foundation mo shot performan These successo that can effectively c

that can effectively cover the data distribution. Monocular Depth Estimation (MDE), which is a fundamental problem with broad applications in robotics [65], autonomous driving [63, 79], virtual reality [47], *etc.*, also requires a foundation model to estimate depth information from a single image. However, this has been underexplored due to the difficulty of building datasets with tens of millions of depth labels. MiDaS [45] made a pioneering study along this direction by training an MDE model on a collection of mixed

Raw video

MiDaS (Previous best)

Depth Anything (Ours)



https://depthanything.github.io



## Single image depth estimation

Obtaining training data for deep learning models in the wild is nowadays possible
Single-image depth estimation models can be effectively trained on such data



MiDaS Depth Estimation is a machine learning model from Intel Labs for monocular depth estimation. It was trained on up to 12 datasets and covers both in-and outdoor scenes. Multiple different MiDaS models are available, ranging from high quality depth estimation to lightweight models for mobile downstream tasks



Ranftl et al. Towards Robust Monocular Depth Estimation: Mixing Datasets for Zero-shot Cross-dataset Transfer. TPAMI 2020

#### Single image depth estimation

- ✓ Obtaining training data for deep learning models in the wild is nowadays possible
- ✓ Single-image depth estimation models can be effectively trained on such data
- X It's challenging to collect data that capture the diversity of the visual world to ensure generalization
- XRGB+ depth data are difficult to collect (Kinect is limited to indoor use, LiDAR are expensive and produce only a sparse depth map)
- X These methods can be easily fooled-out by out-of-distribution samples



Picture from artedelporfido.wordpress.com

Depth map from MegaDepth [1] megadepthdemo.pythonanywhere.com

# Do NN learns from the same visual cues used by humans?

**Explaining depth estimation** 



It is crucial to understand how NNs estimate depths to safely apply them in critical application as autonomous driving...

#### NEW VIDEO



DRIVERLESS UBER CAR INVOLVED IN CRASH IN TEMPE POLICE SAY OTHER DRIVER FAILED TO YIELD



#### **Understanding single image depth estimation**

It is crucial to understand how NNs estimate depths in order to safely apply them in critical application as autonomous driving...

- 1. Which are the most *relevant visual cues* in image?
- 2. How **biased** are depth values in presence of specific objects, shadows, camera orientations?
- 3. How *reliable* are depth values?

## Which pixels of an image *I* are relevant for depth estimation?

Cast the question as an optimization problem:

select a mask M with the smallest set of pixels from which N, a target CNN, produces the maximally similar depth  $\hat{Y} = N(I \odot M)$  to the original output Y = N(I).

in formulas

 $\min \ell(Y, \hat{Y}) + \lambda ||M||_0$ 

The idea is that CNNs can infer depth map equally well from a selected set of sparse pixels, as long as they are relevant to depth estimation. Image I

Masked  $I \odot M$ 



Hu et al., Visualization of Convolutional Neural Networks for Monocular Depth Estimation, ICCV, 2019

## Visualization of CNN for depth estimation

In practice, this problem requires to optimize the output of the CNN with respect to its input that can lead to noisy visualization or even to adversarial examples. Thus:

- Rather than directly optimizing the elements of *M*, obtain the mask by processing *I* via a network *G*,
- Relax the entries of the matrix to be in [0,1]

thus we have the following problem:

$$\min_{\mathbf{G}} \ell(D, \widehat{D}) + \lambda ||G(I)||_1$$





Hu et al., Visualization of Convolutional Neural Networks for Monocular Depth Estimation, ICCV, 2019

The network concentrate on edges, but with some differences





Comparison of accuracy of depth estimation when se- lecting input image pixels using M and using the edge map of input images.

The network concentrate on edges, but consider some edge that are important for the understanding the 3D geometry and neglects others



The network concentrate on edges, but consider some edge that are important for the understanding the 3D geometry and neglects others



Not boundary alone but filled region is highlighted for small objects.

The CNNs recognize the objects and somehow utilize it for depth estimation.





By using different losses we get different results



Emphasis on surfaces

Emphasis on objects & straight edges



The guard rail is relevant strong edge



The white lines are strong edges but are not relevant

A lot of attention near vanishing ponts







A lot of attention near vanishing ponts

#### **Biases in training set?**

Being completely data driven, depth estimation from a single image might inherits the **biases** encoded in the training set.

Let's investigate how some cues (e.g., relative position, apparent size...) affect depth estimation.

Understanding this aspect is crucial for the generalization of the model.





Dijk, Tom van, and Guido de Croon. "How do neural networks see depth in single images?." CVPR 2019

## **Geometric interlude**



We build a simplified **geometric model** and do not consider aperture, exposure, lens distortion...



uca Magri

Dürer, Underwey-sung der Messung

8-3-15191



#### **Pin-hole camera geometry**

Is described by its optical center C and the image plane  $\phi$ .

The distance of the image plane from C is the *f*, the focal length.

The relation between *M* the 3D coordinates of a scene point and *m* the coordinates of its projection onto the image plane is described by the perspective projection



#### **Perspective equations from triangle similarity**

Fix a Cartesian coordinate system  $\{\gamma_x, \gamma_y, \gamma_z\}$  in the optical center, with  $\gamma_z$  perpendicular to the image plane. By similar triangles,  $M = (X_M, Y_M, Z_M)$  is mapped to point  $m = (\frac{f X_M}{Z_M}, \frac{f Y_M}{Z_M})$ 

$$\boldsymbol{M} = (X_M, Y_M, Z_M) \mapsto \boldsymbol{m} = (x_m, y_m), \text{ where } \begin{cases} x_m = f X_M / Z_M \\ y_m = f Y_M / Z_M \end{cases}$$



#### **Camera projection equations are non linear**

**Perspective:** division by  $Z_M$  is responsible of perspective effects. The size of images in the image plane actually depends on their depth in the scene (*i.e.*, distance from the camera center)

 $\begin{cases} x_m = f X_M / Z_M \\ y_m = f Y_M / Z_M \end{cases}$ 

This is not a linear mapping. But we can represent it linearly using homogeneous coordinates

#### **Vanishing points**

Parallel lines in 3D space appear to converge towards the horizon. The line of horizon is formed by infinitely distant points or "vanishing direction".
# **Apparent size**

The **apparent size** of objects are strong visual cues that can be used by a network.

If the object size *H* is known, given the apparent size *h* and the focal distance, it is possible to compute the depth as  $Z = \frac{f}{h}H$ 



# **Vertical position (in terms of horizon)**

Also, the vertical position is an important cue.

If the camera position is known and assuming a flat plane (as in KITTI), the distance can be computed in terms of the height of horizon  $y_h$  as:

$$Z = \frac{f}{(y - y_h)}Y$$



Cropped cars are overimposed with ground contact point at (x, y) and relative depth Z.

When moving to Z', scale factor s and new ground contact point (x', y') can be obtained by knowing the horizon height  $y_h$ .

We can modify the position and the apparent size of the white car in a principled manner.



What happen when we use an apparent size that does not conform with the position and viceversa?

Apparent size is fixed, but position changes. Can you guess the result?





The wrong apparent size doesn't have a great impact on the depth estimates.

According to the apparent size alone this should be a close object, but it should be far according to the position. Is predicted as far

Position is fixed, but apparent size changes... can you guess the result?



Position is fixed, but apparent size changes... can you guess the result?



According to the apparent size alone this should be a far object, but it should be close according to the position. Is predicted as close

# **Position is a stronger visual cue!**



Note that the use of vertical position as a depth cue implies that the networks have some knowledge of the camera's **pose**...

# **Geometric interlude**

Camera and poses

We have chosen:

- a 3D reference frame in the camera center;
- a 2D reference frame in the center of the image;

The projection matrix can be generalized to account for other choices of the reference systems.





1 From world reference frame to camera reference frame using a roto-translation

 $\boldsymbol{M} \mapsto \boldsymbol{R}\boldsymbol{M} + \boldsymbol{t}$ 



Camera reference system

From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix

 $\boldsymbol{M} \mapsto R\boldsymbol{M} + \boldsymbol{t} \mapsto \hat{P}(R\boldsymbol{M} + \boldsymbol{t})$ 



From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix

word r.f. camera r.f. image r.f.  $M \mapsto GM \mapsto \widehat{P}GM$ 

**External orientations:** 

Changing coordinates in space is equivalent to multiplying the matrix P to the right by a 4×4 matrix

$$G = \begin{bmatrix} R & \mathbf{t} \\ 0 & 1 \end{bmatrix}$$

composed by a rotation matrix *R* and a translation vector *t*. It describes the position and the attitude of the camera with respect to the external reference system. It depends on six parameters called external orientations.



From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix
 Express the image point in a different image reference system

 $\mathbf{M} \mapsto \mathbf{G}\mathbf{M} \mapsto \widehat{P}\mathbf{G}\mathbf{M} \mapsto K \ \widehat{P}\mathbf{G}\mathbf{M}$ 



From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix
 Express the image point in a different image reference system

 $M \mapsto GM \mapsto \hat{P}GM \mapsto K \hat{P}GM$ 

2D points in the image plane and 2D point in image coordinates differ by an offset and are expressed in pixels and may have an aspect ratio  $\neq 1$ . These can be accommodated in the camera projection equations

$$\begin{cases} x_m = \sigma_x \frac{X_M}{Z_M} + c_x \\ y_m = \sigma_y \frac{Y_M}{Z_M} + c_y \end{cases}$$



From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix
 Express the image point in a different image reference system

 $\mathbf{M} \mapsto \mathbf{G}\mathbf{M} \mapsto \widehat{P}G\mathbf{M} \mapsto K\widehat{P}G\mathbf{M}$ 

**Camera calibration matrix:** 

In matrix form, this is equivalent of multiplying the matrix P to the left by a  $3 \times 3$  matrix K representing an affine transform. It is customary to include also the focal length (providing a uniform scaling)

$$K = \begin{bmatrix} \alpha_u & s\alpha_u & c_x \\ 0 & r\alpha_u & c_y \\ 0 & 0 & 1 \end{bmatrix}$$

It depends on the *interior parameter*.

- Focal length  $\alpha_u$  expressed in pixel units
- Principal point  $(c_x, c_y)$  (image center)
- Aspect ratio *r* (typical value 1)
- Skew *s* (typical value 0)



From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix
 Express the image point in a different image reference system

## $M \mapsto GM \mapsto \hat{P}GM \mapsto K\hat{P}GM$

#### Camera calibration matrix:

In matrix form, this is equivalent of multiplying the matrix P to the left by a  $3 \times 3$  matrix K representing an affine transform. It is customary to include also the focal length (providing a uniform scaling)

$$K = \begin{bmatrix} \alpha_u & s\alpha_u & c_x \\ 0 & r\alpha_u & c_y \\ 0 & 0 & 1 \end{bmatrix}$$

It depends on the *interior parameter*:

- Focal length  $\alpha_u$  expressed in pixel units
- Principal point  $(c_x, c_y)$  (image center)
- Aspect ratio *r* (typical value 1)
- Skew *s* (typical value 0)

#### Image cords $\widetilde{x}$

- Accessible
- Are measured in the digital image in pixels

Normalized image cords (NIC)  $\tilde{p} = K^{-1}\tilde{x}$ 

- Not accessible without the knowledge of K
- Normalized image coordinates would be measured on an ideal image plane at unit distance from the camera center. Their unit is the same of 3D points.

From world reference frame to camera reference frame using a roto-translation
 Project from camera reference frame to image plane using the projection matrix
 Express the image point in a different image reference system

 $\boldsymbol{M} \mapsto \boldsymbol{G}\boldsymbol{M} \mapsto \boldsymbol{\hat{P}}\boldsymbol{G}\boldsymbol{M} \mapsto \boldsymbol{K}\boldsymbol{\hat{P}}\boldsymbol{G}\boldsymbol{M}$ 

 $P = K[I|\mathbf{0}]G = K[R|\mathbf{t}]$  $\zeta \,\tilde{x} = P \,\tilde{X}$ 

#### **Remarks:**

- $\circ$  *P* has rank 3 since is a 3×4 matrix.
- *KR* is non singular, since *K* is upper triangular with nonzero diagonal and *R* is a rotation matrix
- The Right Null Space of the projection matrix is the camera center (the point for which the projection is not defined)

Does the NN assume a fixed camera pose or estimate this on the fly?

This is strictly related to the location of the **horizon** and of the **vanishing points** 



Does the NN assume a fixed camera pose or estimate this on the fly?

This is strictly related to the location of the **horizon** and of the **vanishing points** 



Vanishing points are directly related with the orientation *R* of the camera



Does the NN assume a fixed camera pose or estimate this on the fly?



This is strictly related to the position of the horizon and of the vanishing points that depends on the orientation of the cameras

Does the NN assume a fixed camera pose or estimate this on-the-fly?

#### Roll

• A different roll is simulated



Pitch



• A different pitch is simulated



cropping image with +/-10 degrees rotation



cropping images with +/-30 pixels vertical offset.



Does the NN<sup>1</sup>assume<sup>1</sup> & fixed camera pose or estimate this on-the-fly? True relative distance [-]

## Roll

- FOIT
- A different roll is simulated
- Estimate roll angle from depth map

Pitch



- A different pitch is simulated.
- Estimate horizon by fitting a line at infinite depth (0 disparity).

#### The network **underestimate** both the roll and the pitch



Does the NN assume a fixed camera pose or estimate this on-the-fly?

#### Roll

- A different roll is simulated
- Estimate roll angle from depth map

Pitch



- A different pitch is simulated.
- Estimate horizon by fitting a line at infinite depth (0 disparity).

The network underestimate both the roll and the pitch

The underestimation of the horizon impact the estimation of the depth (measured in terms of disparity).

The networks look at the vertical image position rather than their distance to the horizon, since the latter does not change when the images are cropped



## **Obstacles**

- 1. only the ground contact point matter
- 2. no information about the object scale is required



Do you think the NN would be able to estimate the depth of the fridge and of the dog?



#### **Obstacles**



**No**! Out of distribution objects are not recognized! The network struggle in finding the ground contact and to segment the object to fill in the depth.

#### **Texture**

#### What matters is the ground contact point!



Objects with unfamiliar shapes, either with or without color, as long as their **gorund contact point** can be located effectively are detected and their depth is predicted based on their lower extent.

#### **Texture**

#### What matters is the ground contact point!



By removing the inner texture of the object, it remains detected in case of a strong bottom edge.

#### **Shadows**

Varying the thickness and intensity of the bottom edge impacts on estimated depth. Objects with thick and dark bottom edges are detected.

This suggests that the networks learn to exploit shadows...



Adding shadows to pasted objects make them appear in the depth map as well.



A naïve uncertainty estimate can be obtained as a post-processing:

- Estimate two depth maps one from the input image and one from a flipped version
- Measure the difference

This provide an estimate of the depth uncertainty



# Aleatoric and epistemic uncertainty

Interestingly Kendall and Gal distinguish between two typo of uncertainty:

• Aleatoric uncertainty captures noise inherent in the observations.

It's important for:

- Large scale data, where epistemic uncertainty is explained away,
- *Real-time applications,* to bypass expensive Monte Carlo computations.
- Epistemic uncertainty accounts for uncertainty in the model uncertainty which can be explained away given enough data.

It's important:

- Small datasets where the training data is sparse.
- Safety-critical applications, because epistemic uncertainty is required to understand examples which are different from training data,



Kendall and Gal. "What uncertainties do we need in bayesian deep learning for computer vision?." NIPS 2017



- Aleatoric uncertainty captures noise inherent in the observations.
  is modeled by placing a distribution over the output of the model.
  We are interested in how this distribution change w.r.t. the input.
- Epistemic uncertainty accounts for uncertainty in the model

#### Higher for

- large depths,
- reflective surfaces,
- occlusion boundaries









Kendall and Gal. "What uncertainties do we need in bayesian deep learning for computer vision?." NIPS 2017

# **Understanding single image depth estimation**

It is crucial to understand how NNs estimate depths in order to safely apply them in critical application as autonomous driving...

#### 1. Which are the most *relevant visual cues* in image?

- It depends on the type of images indoor/outdoor, mainly a subsets of **edges** and **vanishing points**
- 2. How **biased** are depth values in presence of specific objects, shadows, camera orientations?
  - The **vertical position** is more important than the apparent size
  - Depth depends on the pose of the camera, but changes to the pose are not fully accounted for
  - Objects that do not appear in the training set can be detected, but this detection is not always reliable and depends on factors such as the **presence of a shadow** under the object.
- 3. How *reliable* are depth values?
  - Depth estimation can be fooled by out of distribution objects (epistemic uncertainty)
  - And are typically less reliable on distant objects and at boundaries of objects
  - Several methods exists to assess the reliability of depth estimates





https://github.com/andreadalcin/DNN3D

Let's try to estimate depth from a single image using AdaBin A Unet-like architecture with adaptive bin of depths

- You can download the pretrained models "AdaBins\_nyu.pt" and "AdaBins\_kitti.pt"
- You can download the predicted depths in 16-bit format for NYU-Depth-v2 official test set and KITTI Eigen split test set

# Estimating depth from stereo

Geometric supervision


# Acquiring target 3D data is difficult

#### Don't work outside



#### Missing moving objects



#### Sparse measurements

#### Credits Clément Godard

## **Stereoscopy**

Around 1830, the stereoscope. A couple of two-dimensional images captured from a slightly different perspective, could be recombined by the brain to provide a three-dimensional image.

Special stereoscopic cameras were developed to take the left and right images simultaneously, with two lenses separated by around the same distance as human eyes.







## Motion is a strong cue to make depth estimation not (so) ambiguous!



## **Calibrated stereo pair**

The baseline is parallel to both image planes is known.





## **Calibrated stereo pair**

When the camera are calibrated (e.g., we know the focal length f and the baseline b), it is possible to deduce the coordinates Z, from binocular disparity (u' - u):

$$\begin{cases} \frac{f}{Z} = \frac{-u}{X} \\ \frac{f}{Z} = \frac{-u'}{X-b} \end{cases}$$

from which we obtain  $Z = \frac{bf}{u'-u}$ .

Note that when b is unknown, 3D reconstruction is possible only up Z to a **scaling factor**.



Binocluar disparity: the difference in image location of an object seen by the left and right cameras.

The key observation is that close objects have a larger disparity than further ones

From disparity it's possible to recover the depth.

http://vision.middlebury.edu/stereo/data/



Binocluar disparity: the difference in image location of an object seen by the left and right cameras.

The key observation is that close objects have a larger disparity than further ones.

From disparity it's possible to recover the depth.

http://vision.middlebury.edu/stereo/data/



# **Disparity Map**

Estimate **at each image point** *x*, the depth of the scene point *X* as inversely proportional to the displacement between *u* and *u*'

When the cameras are parallel, then the search is much more convenient, as it has to be performed row-wise only



When the stereo camera are calibrated (know focal length and baseline), knowing the disparity is equivalent to knowing the depth. They are inversely proportional

# What if camera are not parallel? No problem!



## **Stereo rectification**

Let's write the new cameras in term of their centers of projection:

$$P_n = K[R \mid -RC], P'_n = K[R \mid -RC']$$
  
The rotation is the same for the new cameras:  $R = \begin{bmatrix} r_1^T \\ r_2^T \\ r_3^T \end{bmatrix}$ 



## **Rectification**

After rectification images are parallel to the baseline.

The idea is to define two new projection matrices  $P_n$ ,  $P_n'$  obtained by rotating the cameras and keeping fixed the centers of projection.

Every point *M* is mapped to  $m_o \cong P_o M$ ,  $m_n \cong P_n M$ .

$$\begin{cases} M = C + \lambda [P_{o\ 1:3}^{-1}m_o|0]^{\mathsf{T}} \\ M = C + \lambda [P_{n\ 1:3}^{-1}m_n|0]^{\mathsf{T}} \end{cases}$$



This is a 3x3 invertible matix: an homography that depends on the camera parameters

The trick is to pose the problem as an image reconstruction one.

### **Pretext task: View synthesis**

- Given an image
- Given the 3D scene (but in our case we want to estimate this!)
- Given the displacement of the cameras (in general the relative pose)

Synthetize a novel image form the point of view defined by the relative pose



In practice, the network learn just to move each pixel by the right horizontal displacement by looking at several left-right pairs. Hence the network has an internal understanding of disparity and hence of depth.

The training set is given by pair of RGB images  $TR = \{(I_L, I_R)\}$ , the depth is no required! The loss is simply image reconstruction. It's a self-supervised problem.



Left Image



Right image

Let's start again with a naïve encoder-decoder model



It works! Hovewer depth perception is latend and we need a way to extract it.

We need an **interpretable** internal representation. Since we are working with a calibrated stereo rig, the obvous choice is disparity.

## **Image reconstruction as supervision: Deep 3D**

Introduce a *differentiable* way to take  $I_L$  and render a novel view close to  $I_R$ .





Xie, Junyuan, Ross Girshick, and Ali Farhadi. "Deep3d: Fully automatic 2d-to-3d video conversion with deep convolutional neural networks." ECCV, 2016.

Luca Magri 2024

# **Image reconstruction as supervision: Deep 3D**

Introduce a *differentiable* way to take  $I_L$  and render a novel view close to  $I_R$ .

- 1. Each pixel predicts a discrete probability distribution over disparity (via softmax)
- 2. Probabilities are used as weights to blend shifted  $I_L$  into the reconstructed  $I_R$
- ✓ Work better than predicting disparity directly
- X Memory consuming: for large image you must represent all the disparities
- X No single value disparity predicted: noisy result







Xie, Junyuan, Ross Girshick, and Ali Farhadi. "Deep3d: Fully automatic 2d-to-3d video conversion with deep convolutional neural networks." ECCV, 2016.



- 1. Predict the depthmap of  $I_L$
- 2. Use the inverse depth as a disparity to wrap  $I_R$
- 3. Minimize the reconstruction error between the warped image and  $I_L$
- Warping is not differentiable; the authors propose several ad-hoc strategy to
   Poor quality

You can make this step differentiable to make it easier to optimize:

- Backward mapping
- Bilinear interpolaiton

Garg, Ravi, et al. "Unsupervised cnn for single view depth estimation: Geometry to the rescue." ECCV 2016.

### Forward mapping

Where so source pixel go?







#### Backward mapping

Where do target pixel comes from?



0	0	0	0
1	1	1	0
1	1	1	0
0	0	0	0

Disparity



### Forward mapping

Where so source pixel go?



Target



#### Backward mapping

Where do target pixel comes from?



	-		
0	0	0	0
1	1	1	0
1	1	1	0
0	0	0	0

Disparity



### Forward mapping

Where so source pixel go?







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Disparity



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Disparity



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Disparity



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Where so source pixel go?



Target



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Where do target pixel comes from?



Disparity



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Where so source pixel go?



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Disparity



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#### Target



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Disparity



## Forward mapping

Where so source pixel go?



Target



### Backward mapping

Where do target pixel comes from?



Disparity



## Forward mapping

Where so source pixel go?



Target



### Backward mapping

Where do target pixel comes from?



Disparity



## Forward mapping

Where so source pixel go?



Target



### Backward mapping

Where do target pixel comes from?

0



 1
 1
 1

 1
 1
 1

 0
 0
 0

Disparity

0

0

0



## Forward mapping

Where so source pixel go?



Target



### Backward mapping

Where do target pixel comes from?



Disparity



## Forward mapping

Where so source pixel go?



Target



### Backward mapping

Where do target pixel comes from?

**Disparity S-T** 









Image spatial extent (1D representation)

0

1.1

2.9

0

In general, disparity values can be in floating precision



Image spatial extent (1D representation)



Image spatial extent (1D representation)

Since we are working on 2D we can use bilinear interpolation



Since we are working on 2D spatial extent, let's use bilinear interpolation.

Jarderberg, Max et al. "Spatial transformer networks". Neruisp 2015

Luca Magri 2024

# Image reconstruction as a supervision: Vanilla Monodepth

- Estimate disparity
- Use differentiable bilinear interpolation to render  $I_R$  from  $I_L$



Structured similarity index measure

Image reconstruction Loss

bilinear interpolation

Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017

## Input





Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017
### Vanilla monodepth





Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017

# Monodepth

By enforcing that the left-view disparity map be equal to the projected right - view disparity map







Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017

Operate on both images:

• wrap  $I_L$  to generate  $I_R$  & wrap  $I_R$  to generate  $I_L$ 

Loss





Enforce consistency between left and right disparities

### **Left-Right disparity Loss**

Loss



Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017

#### **Smoothness Loss**



Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017



Godard, Clément, Oisin Mac Aodha, and Gabriel J. Brostow. "Unsupervised monocular depth estimation with left-right consistency." CVPR. 2017

U-net architecture

- Fully convolutional
- Skip connections
- Fast ~30fps on a Titan X
- Multiscale generation and loss:
  - Reconstruct loss at each stage
  - Upsample the depth and then reconstruction losses at high res, reducing copying texture artefacts



Godard, Clément, et al. "Digging into self-supervised monocular depth estimation." Proceedings of the IEEE/CVF international conference on computer vision. 2019



# **Challenges: occlusions**



# **Challenges: occlusions**







#### How to deal with occlusions?

- Postprocessing
- Predict occlusion mask
- Use more than two views

### Recap

- UNet-like architectures.
- We framed the depth prediction problem as an image reconstruction one.
- Differentiable parametric image generation is easily achieved via bilinear sampling.
- Good results are achieved using multiscale, robust photometric losses, and

# Monocular supervision



In stereo configuration, cameras that does not rotate and moves by pure translation parallel to the image plane. This results in displacement along horizontal lines



Disparity

What happen if we have a more general motion?



In stereo configuration, cameras that does not rotate and moves by pure translation parallel to the image plane. This results in displacement along horizontal lines

Disparity



In stereo configuration, cameras that does not rotate and moves by pure translation parallel to the image plane. This results in displacement along horizontal lines



Disparity

What happen if we have a more general motion?



In stereo configuration, cameras that does not rotate and moves by pure translation parallel to the image plane. This results in displacement along horizontal lines

Disparity



#### What happen if we have a more general motion?



**Optical flow** 



# **Optical flow**







Optical flow is computed enforcing the brightness consistency assumption: I(x, y, t) = I(x + u, y + v, t + dt)

This is not always satisfied due to:

- Occlusions
- Non Lambertian objects
- Perspective effects

Images from Isaac Berrios

## **Optical flow**



#### I(:,:,t+dt)

Images from Isaac Berrios



Optical flow is computed enforcing the brightness consistency assumption: I(x, y, t) = I(x + u, y + v, t + dt)

First order expansion:

$$\nabla I(x, y, t)^{\top} \begin{bmatrix} u \\ v \end{bmatrix} + \partial_t I(x, y, t) = 0$$

This is the projection of *d* along the spatial gradient. The motion can be measured only along the brightness gradient (aperture problem)

### **Aperture problem**







# **Computing the optical flow – sketch of the ideas**

The brightness consistency provide a single equation in two unknown (u, v).

#### Traditional approach:

Tomasi and Kanade algorithm assume that the optical flow is constant in a small  $n \times n$  window in order to accumulate enough constraints, hence they solve a overconstrained linear system

#### Deep learning approach:

- Supervised vanilla
  - GT data comes from 3D scenes or synthetic 3D dataset
  - Direct prediction using an Encoder-Decoder
  - Usually, multiple encoder and decoder are stacked to have a corse to fine refinement



Image pairs

# **Computing the optical flow – sketch of the ideas**

The brightness consistency provide a single equation in two unknown (u, v).

#### Traditional approach:

Tomasi and Kanade algorithm assume that the optical flow is constant in a small  $n \times n$  window in order to accumulate enough constraints, hence they solve a overconstrained linear system

#### Deep learning approach:

- Supervised vanilla
- Iterative approaches

Use a subnetwork to iteratively refine and update the residuals of the optical flow



Image pairs

# **Computing the optical flow – sketch of the ideas**

- Feature encoder that extract features from both input images (context encoder extract feature only from the first image)
- Context encoder to maintain high details
- A correlation layer which build a 4D correlation volume + spatial pyramid pooling (to perform correlation at different scales)
- An update operator which recurrently update the optical flow



雪 Teed, Zachary, and Jia Deng. "Raft: Recurrent all-pairs field transforms for optical flow." ECCV 2020

### Let's go back to our problem



Optical flow



# **Geometric interlude**

Epipolar geometry

A unoclluded 3D point  $\widetilde{X} = (X, Y, Z, 1)^T$  is projected to the left and right image as  $\widetilde{x}_{\ell} = (u_{\ell}, v_{\ell}, 1)^T$  and  $\widetilde{x}_r = (u_r, v_r, 1)^T$ , by

$$\zeta_{\ell} \widetilde{\boldsymbol{x}}_{\ell} = P_{\ell} \widetilde{\boldsymbol{X}} \\ \zeta_{r} \widetilde{\boldsymbol{x}}_{r} = P_{r} \widetilde{\boldsymbol{X}}$$

where  $P_{\ell}$  and  $P_{r}$  denotes the left and the right camera matrix respectively.

Points  $\widetilde{x}_{\ell} \leftrightarrow \widetilde{x}_{r}$  are called corresponding points.



- Baseline: the line passing through the camera centers
- Epipolar plane: the plane containg *X* and the baseline
- Epipoles: the intersection points  $e_{\ell}$  and  $e_{r}$  of the image planes and the baseline
- Epipolar lines: lines  $l_{\ell}$ ,  $l_{r}$  intersection of the epipolar plane and the image plane



Given a point  $\tilde{x}_{\ell}$ , one can determine the epipolar line in the right image on which the corresponding point  $\tilde{x}_r$ , must lie.

The equation of the epipolar line can be derived geometrically, as the projection of the optical ray of  $\tilde{x}_{\ell}$  onto the right image plane:



This is the equation of a line  $l_r$  through the right epipole and the image point  $P_{r \ 1:3}P_{\ell \ 1:3}^{-1}\widetilde{x}_{\ell}$  which represents the projection onto the right image plane of the point at infinity of the optical ray.

The left epipolar line can be derived similarly.

The line  $l_r$  joining  $e_r$  and  $P_{r \ 1:3}P_{\ell \ 1:3}^{-1}\widetilde{x}_{\ell}$  can be represented in terms of the cross product

 $\boldsymbol{l}_r \equiv \boldsymbol{e}_r \times P_{r \ 1:3} P_{\ell \ 1:3}^{-1} \widetilde{\boldsymbol{x}}_{\ell}$ 

$$\boldsymbol{l}_r \equiv [\boldsymbol{e}_r]_{\times} P_{r\,1:3} P_{\ell\,1:3}^{-1} \widetilde{\boldsymbol{x}}_{\ell}$$

The matrix  $F = [e_r]_{\times} P_{r \ 1:3} P_{\ell \ 1:3}^{-1}$  is called **fundamental matrix**.

The epipolar line for a point x is  $l_r = Fx$ . The incidence relation  $\tilde{x}_r \in l_r$  implies  $\tilde{x}_r^T l_r = 0$ and corresponding points have to satisfy

 $\widetilde{\boldsymbol{x}}_{r}^{T}F\widetilde{\boldsymbol{x}}_{l}=0$ 

a point-line relation between two views based only on camera matrices



#### **Fundametal matrix:**

the fundamental matrix *F* is the unique 3×3 matrix rank 2 homogeneous matrix which satisfy  $\mathbf{x}_r^T F \mathbf{x}_l = 0$  for all corresponding points  $\mathbf{x}_r \leftrightarrow \mathbf{x}_l$  in the two images

#### Why rank 2?

Epipolar lines can be seen as the intersection with the image plane of the pencil of planes (epipolar planes) having the baseline as axis.

Consider an epipolar lines  $l' = F x_l$ , The right epipole  $e_r$  lies on this line, so  $e_r^T F x_l = 0$  for all  $x_l$ . This implies that  $e_r^T F = 0$ . Similarly, one can prove that  $F e_\ell = 0$ , this gives an intuition of the reason why F is rank deficient.



#### **Fundametal matrix:**

the fundamental matrix *F* is the unique 3×3 matrix rank 2 homogeneous matrix which satisfy  $\mathbf{x}_r^T F \mathbf{x}_l = 0$  for all corresponding points  $\mathbf{x}_r \leftrightarrow \mathbf{x}_l$  in the two images



**Fundamental matrix:** the fundamental matrix *F* is the unique 3×3 matrix rank 2 homogeneous matrix which satisfy  $\mathbf{x}_r^T F \mathbf{x}_l = 0$  for all corresponding points  $\mathbf{x}_r \leftrightarrow \mathbf{x}_l$  in the two images

Why rank 2?

*F* is a projective map that associate a point in the first image to a line

 $F: \boldsymbol{x}_{\ell} \mapsto \boldsymbol{l}_r$ 

If  $l_{\ell}$  and  $l_r$  are corresponding epipolar lines, then any point  $x_{\ell} \in l_{\ell}$  is mapped to the same line  $l_r$ .

This means there is no inverse mapping and *F* is not of full rank.



The fundamental matrix represents the condition that corresponding points  $x_r \leftrightarrow x_l$  have to satisfy in the camera system.

This property enables computing F from pairs of corresponding points, without having to known  $P_{\ell}$  and  $P_r$ 

If F is the fundamental matrix of the pair of cameras  $P_{\ell}$  and  $P_{r}$ , then  $F^{T}$  is the fundamental matrix of the pair of cameras in the opposite order:  $P_{r}$  and  $P_{\ell}$ .

For any point  $x_{\ell}$  in the right image the corresponding epipolar line is  $l_r = F x_{\ell}$ , similarly  $l_{\ell} = F^T x_r$  identifies the epipolar line corresponding to  $x_r$  in the left image.



### **Essential matrix**

When the interior parameters are known, we can assume that points are in normalized image coordinates (NIC). Using the NIC, the left and the right camera matrices can be chosen as  $P_{\ell} = [I|\mathbf{0}]$  and  $P_r = [R|\mathbf{t}]$ 

By substituting these cameras into the equation of the epipolar line, we get

$$\zeta_r \widetilde{\boldsymbol{p}}_r = \boldsymbol{t} + \zeta_\ell R \widetilde{\boldsymbol{p}}_\ell$$

So, the point  $\tilde{p}_r$  lies on the line through the points t and  $R\tilde{p}_\ell$ :  $\tilde{p}_r^T(t \times R\tilde{p}_\ell) = 0$ 

or

$$\widetilde{\boldsymbol{p}}_r^T[\boldsymbol{t}]_{\times}R\widetilde{\boldsymbol{p}}_{\ell}=0$$

In summary, the relationship between the corresponding image points  $\tilde{p}_{\ell} \leftrightarrow \tilde{p}_{r}$  in NIC is the bilinear form:  $\tilde{p}_{r}^{T} E \tilde{p}_{\ell} = 0$ 

where  $E = [t]_{\times}R$  is called essential matrix and encodes the information on the rigid displacement between cameras. It has five degrees of freedom: a 3D rotation and a 3D translation direction.

### **Input images**





#### Input images from the Adelaide RMF dataset

# **Correspondences and epipolar lines**




### The eight-points algorithm

Given a set of correspondences  $\{x_{i\ell} \leftrightarrow x_{ir}\}$ , we want to determine the matrix F that encodes the bilinear condition:  $x_{ir}^T F x_{i\ell} = 0$ 

This matrix can be recovered using the property of the Kronecker product:

$$\mathbf{x}_{ir}^T F \mathbf{x}_{i\ell} = 0 \Leftrightarrow \operatorname{vec}(\mathbf{x}_{ir}^T F \mathbf{x}_{i\ell}) = 0 \Leftrightarrow (\mathbf{x}_{i\ell}^T \otimes \mathbf{x}_{ir}^T) \operatorname{vec}(F) = 0$$

Every correspondence yields a homogeneous equation in the 9 unknown of *F*. From *n* corresponding points we get the system:

$$\begin{bmatrix} \boldsymbol{x}_{1\ell}^T \otimes \boldsymbol{x}_{1r}^T \\ \boldsymbol{x}_{2\ell}^T \otimes \boldsymbol{x}_{2r}^T \\ \vdots \\ \boldsymbol{x}_{n\ell}^T \otimes \boldsymbol{x}_{nr}^T \end{bmatrix} \operatorname{vec}(F) = 0.$$

The solution of this system is the ker $(A_n)$ . When the points are in general position and n = 8, the solution is determined up to a multiplicative factor. In practice, when more than 8 points are available the solution can be obtained using the SVD.

## The projective reconstruction theorem



One may compute a projective reconstruction of a scene from two views based on image correspondences alone, without knowing anything about the calibration or pose of the two cameras involved. In particular the true reconstruction is within a projective transformation of the projective Luca Magri 2024reconstruction.

### The projective reconstruction theorem



Image credits: Hartely Zisserman

If the calibration matrices are known, the scene can be reconstructed up to a similarity. We still have scale ambiguity

### **Two view Structure from Motion**

- We are given two image of a scene,
- we don't know the poses of the cameras (in some cases we can assume that we do know the intrinsics)
- we want to compute the **3D Structure** of the scene **and** the **motion of the cameras**

There are several approaches to address this problem that produce different outputs:





### **Traditional methods**



- Compute sparse correspondences (handcrafted feature)
- Estimate relative pose between the cameras (robust fitting)
- Triangulate points to get the 3D structure
- Optimize for the position of the triangulated points and for the pose of the cameras (Bundle Adjustment)
- Rectify the cameras
- Compute disparity to get dense correspondences
- Triangulate a dense point cloud







As in stereo self-supervision, rely on view-synthesis.



The source view  $I_S$  is warped via the estimated pose to a novel view  $I_N$ .

The loss is the the photometric error between  $I_N$  and  $I_T$ , and the network learns both the relative depth and the relative pose.



Tinghui Zhou, Matthew Brown, Noah Snavely, David Lowe, Unsu and Ego -motion from Video, CVPR 2017





Tinghui Zhou, Matthew Brown, Noah Snavely, David Lowe, Unsupervised Learning of Depth and Egomotion from Video, CVPR 2017







Tinghui Zhou, Matthew Brown, Noah Snavely, David Lowe, Unsupervised Learning of Depth and Egomotion from Video, CVPR 2017

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Tinghui Zhou, Matthew Brown, Noah Snavely, David Lowe, Unsupervised Learning of Depth and Egomotion from Video, CVPR 2017





### SfM learner





- By using mono-training we can predict the depthmap for a video acquired by a moving camera
- Other and more robust losses can be used: such as ICP loss, motion segmentation loss, or epipolar loss.
- X With respect to stereo self-supervision result are less accurate (edges are not sharp). Why?

More things to learn! (depth and pose) Unknown scale, by estimating the depth from a single image we are addressing an ill-posed problem.



Tinghui Zhou, Matthew Brown, Noah Snavely, David Lowe, Unsupervised Learning of Depth and Egomotion from Video, CVPR 2017

Luca Magri 2024



Ummenhofer, Benjamin, et al. "Demon: Depth and motion network for learning monocular stereo" CVPR. 2017



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isplacement-invariant matching cost learning



low estimation" NIPS 2020

Wei, Xingkui, et al. "Deepsfm: Structure from motion via deep bundle adjustment" ECCV 2020



Supervised SfM assume that a consistent scale of depth and pose can be learned across all input samples, which makes the learning problem harder, resulting in degraded performance and limited generalization.

The idea is to disentangles scale from the network estimation and follow more closely traditional pipelines

	Traditional	Deep + geometry
Correspondences	Sparse handcrafted features	Optical flow
Relative pose	Robust fitting (8/5 points algorithm)	Robust fitting (8/5 points algorithm)
3D scene	Triangulation	Depth estimation



Zhao, Wang, et al. "Towards better generalization: Joint depth-pose learning without posenet." CVPR 2020.

Wang, Jianyuan, et al. "Deep two-view structure-from-motion revisited." CVPR 2021.

### **RanSaC** in short



#### Sample minimal subset

Generate minimal sample model

Is the model interesting? Keep it!

Generate non minimal sample model



Luca Magri 2024



# Removing posenet: two view triangulation as depth supervision

Aligning the depth with the pose

- 1. Select accurate correspondences (taking into consideration epipolar distance, and occlusion mask)
- 2. Reconstruct an up to scale structure using mid-point triangulation (differentiable)

The **loss** of the network is composed by:

- The unsupervised loss for the optical flow,
- The loss between triangulated, and predicted depth,
- The reprojection error (depth map reconstruction + flow error between optical flow and rigid flow generated by depth reprojection),
- Depth smoothness term.



Zhao, Wang, et al. "Towards better generalization: Joint depth-pose learning without posenet." CVPR 2020.

Loss between triangulated and predicted depth

Luca Magri 2024

# **Static scene assumption**

All SfM methods rely on the assumption that the scene is static, thus, as regard moving objects we have two approaches:

Source view

1. Detect and ignore: e.g.:

Target view

Masks estimated by SfMLearner

Explanability mask

AutoHN53khig20stationary pixels by Monodepthv2: ignore pixels in the loss which don't appear to change between images. Allow to ignore whole frames in monocular

videos when the camera stops movin



UNE 16-18 2020

Zhao, Wang, et al. "Towards better generalization: Joint depth-pose learning without posenet." CVPR 2020.

### **Static scene assumption**

All SfM methods rely on the assumption that the scene is static, thus, as regard moving objects we have two approaches:

- 1. Detect and ignore:
- 2. Clever tricks: Mannequin Challenge Dataset



E Li, Zhengqi, et al. "MannequinChallenge: Learning the depths of moving people by watching frozen people." TPAMI 2020.

## **Static scene assumption**

All SfM methods rely on the assumption that the scene is static, thus, as regard moving objects we have two approaches:

- 1. Detect and ignore
- 2. Clever tricks
- 3. Modeling moving objects

Images of a scene with moving object



Dal Cin, Andrea Porfiri, Giacomo Boracchi, and Luca Magri. "Multi-body Depth and Camera Pose Estimation from Multiple Views." ICCV, 2023.

Luca Magri 2024

### Setup:

- The scene is composed by multiple rigid bodies moving independently
- We have a **sparse** set of images (this differs from the previous monodepth approach where the input is typically a video)

### Problem:

If one is able to segment the scene, using SfM pipelines you get indepent reconstruction each in its own scale.

### Goal: We want to reconcile all the reconstruction to the same scale



Dal Cin, Andrea Porfiri, Giacomo Boracchi, and Luca Magri. "Multi-body Depth and Camera Pose Estimation from Multiple Views." ICCV, 2023.

Combine several ingredients that we have seen so far...



Motion segmentation leverages multi-model robust fitting on the optical flow between the two input images to estimate several essential matrices.

- SIFT keypoints are clustered according to object motion (multi-model fitting + synchronization)
- Dense optical flow matches augment the set of keypoints
- For each motion in the scene, we compute essential matrices, and **up-to-scale** camera poses



Dense optical flow

Scale estimation: The monocular depth is used as a prior that can be used to reconcile all the poses in the same scale.

For each image and each moving object, the ratio between the mono and triangulated depth is computed using a Kernel Density Voting.



### Plane sweep

At the core of several traditional plane estimation algorithm, based on photoconsitency Input: an image pair of a source and a target image

- Tentative depth planes parallel to the target are sampled
- For each pixel *u*, and each plane at depth *d*<sub>l</sub> the intersection of the optical ray and the plane is projected onto the source view (the projection *u*<sub>l</sub> depends both on depth and relative pose)
- A photometric error is computed by comparing the image values of pixels u and  $u_l$

The errors can be packaged in a cost volume and the depth of the scene is the surface with the minimum cost





*H*×*W* Size of the target image

## Multi-body plane sweep

This time, each pixel can be projected in different ways according to all the relative motions involved in the dynamic scenes.

All scene motions are considered when constructing the depth cost volume



### Multi-body plane sweep network



# Multi-body plane sweep network

- Receives RGB images and correctly scaled camera poses as input
- Outputs dense depth maps and refined camera poses for each input image
- Includes our multi-body plane sweep algorithm to regress geometrically consistent depths



# Multi-body plane sweep network

Qualitative comparisons on ETH3D and Multi-body Unstructured.

The yellow boxes highlight moving objects reconstructed by our method but not by the state-of-the-art DeepSfM



Reference images

DeepSfM



# Monodepth training

- More abundant data since we can use video sequences
- Multiple viewpoint for reprojection improving the robustness
- Uniform region and moving object must be handled with care



### To sum up

- Depth estimation from a single image is possible
- Compared to other tasks (e.g. object detection, semantic segmentation...) accurate manual annotation is unfeasible
- Geometry come to rescue: self-supervision is possible by exploiting stonger or weaker constraints...

### What's next?

Monocular networks can still be easily fooled!

Although self-supervised techniques allow to increase the amount of training data with low effort, we are far from considering single image depth estimation to be solved.

Conversely to other task, such as Optical Flow and stereo, synthetic images have been rarely used, pretrainig on synthetic samples and fine-tuning on the domain at hand could improve the results.

Even when 3D data are not needed for training, still they are needed for testing.