CNN Anatomy and Training

Giacomo Boracchi, DEIB, Politecnico di Milano Artificial Neural Networks and Deep Learning AY2023-2024

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Parameters in a CNN

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Convolutional Layers

Convolutional layers "mix" all the input components

The output is a linear combination of **all the values in a region of the input, considering all the channels**

$$a(r,c,1) = \sum_{i,j,k} w^1(i,j,k) x(r+i,c+j,k) + b^1$$

The parameters of this layer are called filters.

The same filter is used through the whole spatial extent of the input



By Aphex34 - Own work, CC BY-SA 4.0, https://commons.wikimedia.org/w/index.php?curid=45659236

Convolutions as MLP

Convolution is a linear operation!

Therefore, if you unroll the input image to a vector, you can consider convolution weights as the weights of a Multilayer Perceptron Network!



What are the differences between MLP and CNNs then?

CNNs has Sparse Connectivity



Weight Sharing / Spatial Invariance

In a CNN, all the neurons in the same slice of a feature map use the same weights and bias: this reduces the nr. of parameters in the CNN.

Underlying assumption: if one feature is useful to compute at some spatial position (x, y), then it should also be useful to compute at a different position (x_2, y_2)



Weight Sharing / Spatial Invariance

If the first layer were a MLP:

- MLP layer: this should have had 28 x 28 x 6 neurons in the output
- MLP layer with sparse connectivity: only 5x5 nonzero weights each neuron
- MLP layer: 28 x 28 x 6 x 25 weights + 28 x 28 x 6 biases (122 304)
- Conv layer: 25 weights + 6 biases shared among neurons of the same layer



Parameter sharing



Parameter sharing



To Summarize

Any CONV layer can be implemented by a FC layer performing exactly the same computations.

The weight matrix W of the FC layer would be

- a large matrix (#rows equal to the number of output neurons, #cols equal to the nr of input neurons).
- That is mostly zero except for at certain blocks where the local connectivity takes place.
- The weights in many of the blocks are equal due to parameter sharing.

... and we will see that the converse interpretation (FC as conv) is also viable and very useful!

The Receptive Field A very important aspect in CNNs

The Receptive Field

One of the basic concepts in deep CNNs.

Due to sparse connectivity, unlike in FC networks where the value of each output depends on the entire input, **in CNN each output only depends on a specific region in the input.**

This region in the input is the receptive field for that output

The deeper you go, the wider the receptive field is: maxpooling, convolutions and stride > 1 increase the receptive field

Usually, the receptive field refers to the final **output unit** of the network in relation to the network input, but the same definition holds for intermediate volumes



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Deeper neurons depend on wider patches of the input (convolution is enough to increase receptive field, no need of maxpooling)



Exercise

Input:

map







Exercise















As we move deeper...

As we move to deeper layers:

- spatial resolution is reduced
- the number of maps increases

We search for higher-level patterns, and don't care too much about their exact location.

There are more high-level patterns than low-level details!



CNN Training

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Training a CNN

- Each CNN can be seen as a MLP, with sparse and shared connectivities)
- CNN can be in principle **trained by gradient descent** to minimize a loss function over a batch (e.g. binary cross-entropy, RMSE, Hinge loss..)
- Gradient can be computed by **backpropagation** (chain rule) as long as we can derive each layer of the CNN
- Weight sharing needs to be taken into account (fewer parameters to be used in the derivatives) while computing derivatives
- There are just a few details missing...

Detail: backprop with max pooling

The gradient is only routed through the input pixel that contributes to the output value; e.g.:



Detail: backprop with max pooling

The gradient is only routed through the input pixel that contributes to the output value; e.g.:



Detail: derivative of ReLU

The ReLU derivative is straightforward



A Breaktrough in Image Classification

The impact of Deep Learning in Visual Recognition Network of the second sec



Many layers!

ILSVRC: ImageNet Large Scale Visual Recognition Challenge

AlexNet / Imagenet Images





Krizhevsky, Alex, Ilya Sutskever, and Geoffrey E. Hinton. "Imagenet classification with deep convolutional neural networks." Advances in neural 37 information processing systems 25 (2012).

How was this possible?

Large Collections of Annotated Data MAGENET



The ImageNet project is a large visual database designed for use in visual object recognition software research. More than 14 million images have been handannotated by the project to indicate what objects are pictured and in at least one million of the images, bounding boxes are also provided.[3] ImageNet contains more than 20,000 categories

From Wikipedia October 2021

J. Deng, W. Dong, R. Socher, L.-J. Li, K. Li and L. Fei-Fei, ImageNet: A Large-Scale Hierarchical Image Database. *CVPR, 2009.* Giacomo Boracchi

Parallel Computing Architectures





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And more recently.... Software libraries

で PyTorch TensorFlow

Google LLC, Public domain, via Wikimedia Commons

PyTorch, BSD <http://opensource.org/licenses/bsd-license.php>, via Wikimedia Commons

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Data Scarcity

Training a CNN with Limited Aumont of Data

The need of data

Deep learning models are very data hungry.

Networks such as AlexNet have been trained on ImageNet datasets containing tens of thousands of images over hundreds of classes
The need of data

This is necessary to define millions of parameters characterizing these networks



Canziani, Alfredo, Adam Paszke, and Eugenio Culurciello. "An analysis of deep neural network models for practical applications." arXiv preprint arXiv:1605.07678 (2016).

The need of data

Deep learning models are very data hungry.

... watch out: each image in the training set have to be annotated!

How to train a deep learning model with a few training images?

- Data augmentation
- Transfer Learning

Limited Amount of Data: Data Augmentation

Training a CNN with Limited Aumont of Data

Aleutian Islands

Messico

Stati Uniti

Steller sea lions in the western Aleutian Islands have declined 94% in the last 30 years.

Canada



Kaggle in 2017 have opened a competition to develop algorithms which accurately count the number of sea lions in aerial photographs

OPPAREC-CNN-Demo

Credits Yinan Zhou

The Challenge

In very large aerial images (\approx 5K x 4K) shot by drones, automatically count the number of sealions per each category



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The Challenge

This problem can be naively casted in a patch-by-patch 6-class classification problem, where we include also background



An Example of CNN predictions







Credits Yinan Zhou https://github.com/marioZYN/FC-CNN-Demo

Data Augmentation

Often, each annotated image represents a class of images that are all likely to belong to the same class

In aereal photograps, for instance, it is normal to have rotated, shifted or scaled images without changing the label



Data Augmentation



Data Augmentation

Data augmentation is typically performed by means of

Geometric Transformations:

- Shifts /Rotation/Affine/perspective distortions
- Shear
- Scaling
- Flip

Photometric Transformations:

- Adding noise
- Modifying average intensity
- Superimposing other images
- Modifying image contrast

Data Augmentation Criteria

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Data Augmentation: Criteria

Augmented versions should preserve the input label

• e.g. if size/orientation is a key information to determine the output target (either the class or the value in case of regression), wisely consider scaling/rotation as transformation

Augmentation is meant to **promote network invariance** w.r.t. transformation used for augmentation

Non-preserving label augmentation



You don't want to introduce transformations that ruin distinctive information of a given class



A network predicting the time from an image of a clock without numbers is not invariant w.r.t rotations

Mixup Augmentation

Augmented copies $\{A_l(I)\}_l$ of an image I live in a **vicinity** of I, and **have the same label** of I

Transformations (photometric or geometric) are *expert-driven*

Mixup is a **domain-agnostic** data augmentation technique

- No need to know which (label-preserving) transformations to use
- mixup trains a neural network on *virtual samples* that are convex combinations of pairs of examples and their labels

Mixup Augmentation

Given a pair of training samples (I_i, y_i) and (I_j, y_j) of drawn at random possibly belonging to different classes, we define

Virtual samples (and their label)

$$\tilde{I} = \lambda I_i + (1 - \lambda)I_j$$

$$\tilde{y} = \lambda y_i + (1 - \lambda)y_j$$

Where $\lambda \in [0,1]$ and y_i , and y_j are **one-hot encoded labels**



https://www.kaggle.com/code/kaushal2896/data-augmentation-tutorial-basic-cutout-mixup

Mixup Augmentation, Intuition

Mixup extends the training distribution by incorporating the prior knowledge that linear interpolations of feature vectors should lead to linear interpolations of the associated targets.

Mixup can be implemented in a few lines of codes and introduces minimal computation overhead.

Mixup in keras: <u>https://keras.io/guides/keras_cv/cut_mix_mix_up_and_rand_augment/</u>

Zhang, H., Cisse, M., Dauphin, Y. N., & Lopez-Paz, D. (2018). Mixup: Beyond empirical risk minimization. ICLR 2018

The Benefits of Data Augmentation

Image Augmentation and CNN invariance

Given an annotated image (I, y) and a set of augmentation transformations $\{A_l\}_l$, we train the network using these pairs $\{(A_l(I), y)_l\}_l$

Through data augmentation we train the network to «become invariant» to selected transformations. Since the same label is associated to I and $A_l(I) \forall l$

Unfortunately:

- invariance might not be always achieved in practice,
- several type of invariance cannot be achieved by synthetic manipulation of images

This sort of data augmentation might not be enough to capture the inter-class variability of images...

Superimposition of targets



Background variations



Background variations



Out of focus, bad exposure



Image Augmentation and Overfitting

Given an annotated image (I, y) and a set of augmentation transformations $\{A_l\}_l$, we train the network using these pairs $\{(A_l(I), y)_l\}_l$

Training including augmentation **reduces the risk of overfitting**, as it significantly increase the training set size.

Note: data augmentation can be implemented as a network layer, such that it is executed on each batch, **thus changing augmented images at each epochs**

Image Augmentation and Class Imbalance

Moreover, data augmentation can be used to compensate for class imbalance in the training set, by **creating more realistic examples from the minority class**

In general, transformations used in data-augmentation $\{A_l\}$ can be also class-specific, in order to preserve the image label





Watch out

If Data-augmentation introduces some «hidden traces» that are classdiscriminative, then the network will learn these to perform detection!

For instance

- Blurring only images of a specific class, makes the network learn that class "*as blurry*", despite the image semantics. This holds for interpolation artifacts as well
- Changing colors / creating inconsistencies / introducing minor padding artifacts in a certain class of images, might create new class-discriminative patterns.

Test Time Augmentation

Test Time Augmentation (TTA) or Self-ensembling

Even if the CNN is trained using augmentation, **it won't achieve perfect invariance** w.r.t. considered transformations

Test time augmentation (TTA): augmentation can be also performed at test time to improve prediction accuracy.

• Perform a few random augmentation of each test image $I = \{A_l(I)\}_l$

 $\Rightarrow \hat{y}$

CNN

- Classify all the augmented images and save the posterior vectors $p_l = CNN(A_l(I))$
- Define the CNN prediction by aggregating the posterior vectors $\{p_l\}$ e.g. $p = Avg(\{p_l\}_l)$

$$I \implies AUG \implies \{A_t(I)\} \implies CNN \implies \{\hat{y}_t\} \implies aggregation \implies \hat{y}$$

Test Time Augmentation (TTA) or Self-ensembling

TTA:

- particularly useful for test images where the model is quite unsure.
- extremely computationally demanding

Need to wisely configure the number and type of transformations to be performed at test time

Test Time Augmentation



Figure source: https://stepup.ai/test_time_data_augmentation/

Augmentation In Keras

Augmentation in Keras

There are multiple **preprocessing layers** to be introduced after the input layer to perform:

- photometric transformations
- geometric transformations

to the image

https://keras.io/api/layers/preprocessing_layers/image_augmentation/

Augmentation Layers

These layers apply random augmentation transforms to a batch of images. They are only active during training.

tf.keras.layers.RandomCrop

tf.keras.layers.RandomFlip

tf.keras.layers.RandomTranslation

tf.keras.layers.RandomRotation

tf.keras.layers.RandomZoom

tf.keras.layers.RandomHeight

tf.keras.layers.RandomWidth

tf.keras.layers.RandomContrast

Preprocessing Layers

Image preprocessing layers, these are active at inference

- Resizing layer
- Rescaling layer
- CenterCrop layer

Augmenting Images

```
Define a simple network that performs a random flip of the input
flip = tf.keras.Sequential([
   tfkl.RandomFlip("horizontal_and_vertical"),
])
```

Invoke this network to apply augmentation to images
flipped_X_train = flip(X_train)
Augmenting Images

You can stuck multiple layers

pack a few augmentation layers in a sequence

augmentationNet = tf.keras.Sequential([

tfkl.RandomFlip("horizontal_and_vertical"),

tfkl.RandomTranslation(0.1,0.1),

tfkl.RandomRotation(0.1),

```
], name='augmentationNet')
```

Invoke this network to apply augmentation to images
augmentated_X_train = augmentationNet(X_train)

Training with data augmentation

You can include augmentation / preprocessing layers directly in the network architecture Note:

- Augmentation layers will be active only during training
- Preprocessing layers will be active also during inference

```
def build_model_with_augmentation(input_shape, output_shape):
    tf.random.set_seed(seed)
```

```
# Build the neural network layer by layer
input_layer = tfkl.Input(shape=input_shape, name='Input')
```

include augmentation layers

```
a = tfkl.RandomFlip("horizontal_and_vertical")(input_layer)
```

- b = tfkl.RandomTranslation(0.1,0.1)(a)
- c = tfkl.RandomRotation(0.1)(b)

```
conv1 = tfkl.Conv2D(...) (c)
```

A bit more of background

Performance measures

and an overview of successful architectures

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Confusion Matrix



Confusion Matrix

The element C(i, j) i.e. at the *i*-th row and *j*-th column corresponds to the percentage of elements belonging to class *i* classified as elements of class *j*



· 0.8

... so, the ideal confusion matrix

Which rarely happens



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Two-Class Classification

Background:

In a two-class classification problem (binary classification), the CNN output is equivalent to a scalar, since

$$CNN(I) = [p, 1-p]$$

being p the probability of I to belong to the first class. Thus, we can write

CNN(I) = p

Then, we can decide that I belongs to the first class when $CNN(I) > \Gamma$

and use Γ different from 0.5, which is the standard.

We require stronger evidence before claiming *I* belongs to class 1.

Changing Γ establishes a trade off between FPR and TPR.

Two-Class Classification

Classification performance in case of **binary classifiers** can be also measured in terms of the **ROC** (receiver operating characteristic) **curve**, which does not depend on the threshold you set for each class

This is useful in case you plan to modify this and not use 0.5

The ideal detector would achieve:

- FPR = 0%,
- TPR = 100%

Thus, the closer to (0,1) the better

The largest the **Area Under the Curve** (AUC), the better

The optimal parameter is the one yielding the point closest to (0,1)



specific parameter

CNN for Quality Inspection

In collaboration with

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Scenario

Chip Manufacturer



Silicon Wafer

Chips / Memories / Sensors are everywere



Monitoring Silicon Wafer Manufacturing Process



Classess of WDM Patterns

Specific patterns in WDMs might indicate problems in the production



Classify WDM to raise prompt alerts

Challenges

- Huge resolution: a WDM as a grayscale would require $\sim 3~{\rm GB}$ to store w in memory
- Very Limited Supervision
- Some defects occur very rarely



Our CNN

Collaboration with life.augmented

Train a deep learning model to identify defective patterns

Defect Patterns



R. di Bella, D. Carrera, B. Rossi, P. Fragneto, G. Boracchi «Wafer Defect Map Classification Using Sparse Convolutional Networks" ICIAP 2019

Data Augmentation is often key..

Collaboration with



R. di Bella, D. Carrera, B. Rossi, P. Fragneto, G. Boracchi «Wafer Defect Map Classification Using Sparse Convolutional Networks" ICIAP 2019

Our CNN



Results







Our system is currently monitoring the largest production line in Agrate and most backend sites



Limited Amount of Data: Transfer Learning

Training a CNN with Limited Aumont of Data

The Rationale Behind Transfer Learning

The typical architecture of a CNN



Very Good Features!

FEN is trained on large training sets (e.g. ImageNet) typically including hundres of classes.



IM GENET

L = 999 output neurons

- 0 tench, Tinca tinca
- goldfish, Carassius auratus
- 2 great white shark, man-eating shark, Carcharodon caharias',

998 ear, spike, capitulum999 toilet tissue, toilet paper, bathroom tissue

Very Good Features!



L = 999 output neurons

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The **output of the fully connected layer** has the same size as the number of classes *L*, and each component provide a score for the input image to belong to a specific class.

This is very task-specific:

- What if I have a *small TR* of images of **cats and dogs** for training?
- What if I want to train a classifier for the six types of sealions?
- Can we use these feature for solving other classification problems?

Transfer Learning



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Transfer Learning



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- 1. Take a powerful pre-trained NN (e.g., ResNet, EfficientNet, MobileNet)
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- 4. «Freeze» the weights of the FEN.
- 5. Train the whole network on the new training data TR

Transfer Learning in the Sealion Case



https://jhui.github.io/2017/03/16/CNN-Convolutional-neural-network/

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Transfer Learning vs Fine Tuning

Different Options:

- Transfer Learning: only the FC layers are being trained. A good option when little training data are provided and the pre-trained model is expected to match the problem at hand
- Fine tuning: the whole CNN is retrained, but the convolutional layers are initialized to the pre-trained model. A good option when enough training data are provided or when the pre-trained model is not expected to match the problem at hand.

Typically, for the same optimizer, **lower learning rates** are used when performing fine tuning than when training from scratches

Best Practice

Typically, to take the most out of a pretrained model:

- Connect a new output layer (having few parameters)
- Transfer Learning: train the output layer only
- Make all the "last layers" trainable
- Fine tuning: train the entire network with a low learning rate
- # Compile the model

ft_model.compile(loss=tfk.losses.BinaryCrossentr
opy(), optimizer=tfk.optimizers.Adam(1e5), metrics='accuracy')

This strategy allows defining good predictions once the output layer has been trained



Transfer Learning In Keras

Where to find pretrained models?

https://keras.io/api/applications/

Available models

Model	Size (MB)	Top-1 Accuracy	Top-5 Accuracy	Parameters	Depth	Time (ms) per inference step (CPU)	Time (ms) per inference step (GPU)
Xception	88	79.0%	94.5%	22.9M	81	109.4	8.1
VGG16	528	71.3%	90.1%	138.4M	16	69.5	4.2
VGG19	549	71.3%	90.0%	143.7M	19	84.8	4.4
ResNet50	98	74.9%	92.1%	25.6M	107	58.2	4.6
ResNet50V2	98	76.0%	93.0%	25.6M	103	45.6	4.4
ResNet101	171	76.4%	92.8%	44.7M	209	89.6	5.2
ResNet101V2	171	77.2%	93.8%	44.7M	205	72.7	5.4
ResNet152	232	76.6%	93.1%	60.4M	311	127.4	6.5
ResNet152V2	232	78.0%	94.2%	60.4M	307	107.5	6.6
InceptionV3	92	77.9%	93.7%	23.9M	189	42.2	6.9
InceptionResNetV2	215	80.3%	95.3%	55.9M	449	130.2	10.0
MobileNet	16	70.4%	89.5%	4.3M	55	22.6	3.4
MobileNetV2	14	71.3%	90.1%	3.5M	105	25.9	3.8
DenseNet121	33	75.0%	92.3%	8.1M	242	77.1	5.4
DenseNet169	57	76.2%	93.2%	14.3M	338	96.4	6.3
DenseNet201	80	77.3%	93.6%	20.2M	402	127.2	6.7
NASNetMobile	23	74.4%	91.9%	5.3M	389	27.0	6.7
NASNetLarge	343	82.5%	96.0%	88.9M	533	344.5	20.0
EfficientNetB0	29	77.1%	93.3%	5.3M	132	46.0	4.9

Importing Pretrained Models in keras...

Pre-trained models are available, typically in two ways:

- **include_top = True:** provides the entire network, including the fully convolutional layers. This network can be used to solve the classification problem it was trained for
- **include_top = False:** contains only the convolutional layers of the network, and it is specifically meant for transfer learning.

Have a look at the size of these models in the two options!

Importing Pretrained Models in keras...

```
from keras import applications
base_model = applications.VGG16(weights =
"imagenet", include_top=False, input_shape =
(img_width, img_width, 3), pooling = "avg")
```
Importing Pretrained Models in keras...

from keras import applications
base_model = applications.VGG16(weights =
 "imagenet", include_top=False, input_shape =
 (img_width, img_width, 3), pooling = "avg")

When **include_top=False**, the network returns the output of a global pooling layer, which can be:

- **pooling = "avg"** Global Averaging Pooling (GAP)
- **pooling = "max**" Global Max Pooling (GMP)
- **pooling = "none"** There is no pooling, it returns the activations

How to extract the feature extraction network?

Actually, for sequential models, you create feature extraction network fen = tfk.Sequential(model.layers[:-2]) fen.output shape >> 128 **Convolution layers** Fully connected layers 256x1 2x2 024x1 1024 096x1

How to extract the feature extraction network?

Actually, for sequential models, you create feature extraction network fen = tfk.Sequential(model.layers[:-2])

Note: each Keras Application expects a specific kind of input **preprocessing**.

For MobileNetV2, call

tf.keras.applications.mobilenet_v2.preprocess_input

on your inputs before passing them to the model. mobilenet_v2.preprocess_input will scale input pixels between -1 and 1.

Transfer Learning in Keras...

Requires a bit of TensorFlow Backend to add the modified Fully connected layer at the top of a pretrained model

Then, before training it is necessary to loop through the network layers (they are in **model.layers**) and then modify the trainable property

for layer in model.layers[: lastFrozen]:
 layer.trainable=False

An example of model loading

```
# load a pre-
trained MobileNetV2 model without weights
mobile = tfk.applications.MobileNetV2(
    input_shape=(224, 224, 3),
    include_top=False,
    pooling='avg',
```

Transfer Learning: adding the new Network Top

Requires a bit of TensorFlow Backend to add the modified Fully connected layer at the top of a pretrained model

Then, before training it is necessary to loop through the network layers (they are in **model.layers**) and then modify the trainable property

Add the classifier layer to the MobileNet

inputs = tfk.Input(shape=(224,224,3))

x = mobile(inputs) # concatenates inputs and the output
of the pretrined network... the entire mobileNet is hand
led as a layer

x = tfkl.Dropout(0.5)(x) **# good to prevent overfitting**

outputs = tfkl.Dense(1, activation='sigmoid')(x) # conne
ct a new output layer

Transfer Learning: setting layers trainable property

Requires a bit of TensorFlow Backend to add the modified Fully connected layer at the top of a pretrained model

Then, before training it is necessary to loop through the network layers (they are in **model.layers**) and then modify the trainable property

for layer in model.layers[: lastFrozen]:
 layer.trainable=False

Image Retrieval From The Latent Space

Feed a test image and compute its latent representation



Latent Representation: Data-Driven Feature Vector

Krizhevsky, Alex, Ilya Sutskever, and Geoffrey E. Hinton. "Imagenet classification with deep convolutional neural networks." NIPS 2012



Retrieve the training images having the closest latent representations



Data-Driven Feature Vector

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Feed a test image and compute its latent representation



Latent Representation: Data-Driven Feature Vector Retrieve the training images having the closest latent representations

The 3- nearest neighborhood of \boldsymbol{x}





Krizhevsky, Alex, Ilya Sutskever, and Geoffrey E. Hinton. "Imagenet classification with deep convolutional neural networks." NIPS 2012

Feed a test image and compute its latent representation



Training Images corresponding to the closest latent representations!



Krizhevsky, Alex, Ilya Sutskever, and Geoffrey E. Hinton. "Imagenet classification with deep convolutional neural networks." Advances in neural information processing systems 25 (2012).

1-NN classification in the latent space

feed the test imate to the fen

image_features = fen.predict(test_image)

feed fen with the entire training set (use batches of 512)
features = fen.predict(X_train_val,batch_size=512,verbose=0)

```
# compute distances (e.g. ell1) between image_featres and features,
distances = np.mean(np.abs(features - image_features),axis=-1)
sortedDistances = distances.argsort()
```

```
# sort images (and labels) according to the distance computed above
ordered_images = X_train_val[sortedDistances]
ordered_labels = y_train_val[sortedDistances]
# associate to image_features the closest image ordered_images[0]
```